kan/sm1 operators reference

3.050615

1 Primitive Operators

1.1 QUIT

```
The bye or QUIT or quit statement terminates the kan/sm1.
```

1.2 Usage

```
The keyword <<Usage>> cannot be found.
Type in ? in order to see system dictionary.
```

1.3 [

```
[ and ] are used to construct an array.
The left bracket [ is an operator that leaves an object called
a mark on the stack. The interpreter puts more objects
until it encounters a right bracket, which creates
an array. So, it is possible to construct an array, for example, in the way
 [  1  2  [ 2 1 roll 3] ] print ==> [1 [2 3]]
```

1.4]

```
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an array. So, it is possible to construct an array, for example, in the way
 [  1  2  [ 2 1 roll 3] ] print ==> [1 [2 3]]
```

1.5 add

```
<< obj1 obj2 add obj3 >>
obj3 is the sum of obj1 and obj2.
If obj1=f1/f2, obj2=g1/g2, then obj3 is given by (g2 f1 + f2 g1)/(f2 g2)
Example:  2 3 add ::  ==> 5
```

1.6 aload

```
<< [f1 f2 ... fn] aload f1 f2 ... fn [f1 ... fn] >>
The primitive aload decomposes an array into the set of the elements.
Example: [(x1+1) (23)] aload length ===> (x1+1) (23) 2
```

1.7 bye

```
The bye or QUIT or quit statement terminates the kan/sm1.
```

1.8 cat_n

```
<< s1 s2 ... sn n cat_n s1s2...sn >>
string s1, s2, ..., sn ; integer n ; string s1s2...sn
The primitive cat_n concatnates the strings(dollars) s1 ... sn.
Example: (ab c) (2) 2 cat_n ===> (ab c2)
```

1.9 cclass

```
<< [super-class-tag, o1, o2, ...] size [class-tag] cclass [class-tag, o1, o2, .... ] >>
```

1.10 closefile

```
<< fd closefile >>
file fd;
cf. file (open a file)
```

1.11 coeff

```
<< f v coeff [exponents coefficients] >>
poly f,v; list of integers exponents; list of poly coefficients;
The primitive coeff returns the array of exponents and
the array of coefficients of the polynomial f with respect to
the variable v.
```

```
The primitive coefficients have not yet removed for a compatibility with the old macro packages.
Note that the data type of each element of exponents is <Poly>(9) and it may cause a trouble when p>0.
cf. dc,  (interger) dc
C-functions: Kparts2, parts2
Example: [(x,y) ring_of_polynomials [[(x) 1 (y) 1]] weight_vector
           0] define_ring
         (x^2+ x y + x). (x). coeff print ;
  ===>  [ [ 2 , 1 ] , [1 , y+1] ]
```

1.12 coefficients

```
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the array of coefficients of the polynomial f with respect to
the variable v.
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Example: [(x,y) ring_of_polynomials [[(x) 1 (y) 1]] weight_vector
           0] define_ring
         (x^2+ x y + x). (x). coeff print ;
  ===>  [ [ 2 , 1 ] , [1 , y+1] ]
```

1.13 copy

```
<< f1 f2 ... fn n copy f1 f2 ... fn f1 f2 ... fn >>
The primitive copy_n duplicates the objects f1 f2 ... fn.
integer n;
Example: (x1+1) 1 copy ===> (x1+1) (x1+1)
<<copy>> copies the values of the objects.  cf. dup
```

1.14 data_conversion

```
<< obj (type?) data_conversion type >>
<< obj (type??) data_conversion type >>
<< obj (key word) data_conversion obj >>
integer type; object obj;
Key words: null, integer, literal, dollar, string, poly, universalNumber,
           ring, numerator, denominator, double, cancel,
           map, orderMatrix, error,
 or [(class) (class-name)].
The primitive reports and converts the data type of obj.
Special combinations of obj and keyword.
   ring (oxRingStructure) data_conversion list
Example: (2) (integer) data_conversion ===> 2
```

1.15 def

```
<< /name object def >>  or  << object /name set >>
The primitive def or set binds the object to the name
Example: /abc (23) def    abc :: ---> (23)
Example: (23) /abc set    abc :: ---> (23)
```

1.16 degree

```
<< f  v  degree  deg >>
poly f,v; integer deg;
deg is the degree of the polynomial f with respect to the variable v.
Example: (x^3 + x h + 1).  (x).  degree :: ---> 3
```

1.17 div

```
<< obj1  obj2 div obj3 >>
obj3 is obj1/obj2
cf. data_conversion (numerator, denominator, cancel)
```

1.18 dup

```
<< obj dup obj obj >>
cf. 1 copy. Dup copies the object by the pointer.
```

1.19 elimination_order

```
<< (v1,...,vm) elimination_order >>
The primitive returns the weight matrix where the variables
v1, ..., vm are most expensive terms.
cf. define_ring, define_qring.
```

1.20 eq

```
<< o1 o2 lt r1  >> or  <<  o1 o2 gt r1 >> or <<  o1 o2 gt r1 >>
integer r1;
These premitives compare objects o1 and o2.
[lt (less than), gt (greater than), eq (equal)]
The result is r1 which is integer object.
Here, 1 means true and 0 means false.
Example:  (abc) (bca) eq ::  ===> 0
```

1.21 error

```
<<error>> causes kan/sm1 error.
<< s error >>   string s;
s is printed as the error message.
```

1.22 eval

```
<< [$key$ arguments] eval >>
key :
```

1.23 exec

```
<< { executable array } exec >>
The primitive exec executes each primitive in the executable
array sequentially.
Example: {1 2 add print pop} exec ;
    ===> 3
```

1.24 exit

```
The keyword <<exit>> cannot be found.
Type in ? in order to see system dictionary.
```

1.25 extension

```
<< obj1 extension obj2 >>
array of object obj1; object obj2;
The first element of the obj1 should be the key word tag.
<< extension >> is used to install a new function to a system. cf.ext.c and plugin/
  [(parse) string] extension result-integer
  [(chattr) num literal] extension result-object
  [(chattrs) num ] extension result-object
  [(date)] extension date-string
  [(defaultPolyRing) num ] extension result-object
  [(flush) ] extension null
  [(getAttribute) obj key] extension value
  [(getAttributeList) obj] extension attrList
  [(getpid) ] extension result-integer
  [(getenv) envName] extension valueOfEnvName
  [(gethostname) ] extension myhostname
  [(stat) fname] extension v
       v = [null,[(error no), p]] or [0, [size ]]
  [(forkExec) argList fdList sigblock] extension pid
  [(getattr) literal] extension attr
  [(getchild)] extension listOfPid (generated by forkExec)
```

```
  [(keywords) ] extension array-of-names-of-primitives
  [(nobody) ] extension null
  [(newMatrix) m n] extension mat
  [(newVector) m ] extension vec
  [(getUniqueFileName) path] extension newName
  [(or_attr) atr literal] extension new_value
  [(or_attrs) atr ] extension result-obj
  [(outputObjectToFile) path obj] extension null
  [(ostype)] extension list
  [(quiet) flag] extension int
  [(setAttribute) obj key value] extension new-attributed-obj
  [(setAttributeList) obj attrList] extension new-attributed-obj
  [(stringToArgv) sobj] extension decomposed_str  cf. to_records
  [(stringToArgv2) sobj separator] extension decomposed_str  cf. to_records
  [(read) fd size] extension string
  [(regexec) regular_expression stringArray flags(opt)] extension list
  [(regionMatches) string stringArray] extension list
  [(traceClearStack)] extension null
  [(traceShowStack)] extension str
  [(traceShowScannerBuf)] extension str
  [(unlink) fname] extension r
See also plugin-* in ?? by [(plugin)] usages ::
See also (extension-examples) usage ::
```

1.26 file

```
<< filename mode file fd >>
string filename, mode; file fd;
It opens the <<filename>> with the <<mode>>. <<fd>> is the
file descripter and is used in writestring and closefile.
If filename part is an integer, it calls fdopen() and returns the file descripter.
cf. closefile, writestring, pushfile
```

1.27 for

```
<<init inc limit {executable array} for >>
integer init inc limit;
Repeat the executable array.
Example: [ 1 1 3 {(a)} for] ::---> [1 (a) 2 (a) 3 (a)]
```

1.28 gbext

```
<< obj1 gbext obj2 >>
array of objects obj1;The first element of the obj1 should be the key word tag.
<< gbext >> is used to call auxiliary functions for g-basis computation.
  [(divByN) poly1 n(universalNumber)] gbext [qpoly rpoly]
     where poly1 = n*qpoly+rpoly.
     (see also cancelCoeff)
  [(exponents) poly type ] gbext array
    example: type == 0    x,y,Dx,Dy
```

```
            type == 1    x,y,Dx,Dy,h,H
            type == 2    x,y,Dx,Dy,h  --- default.
  [(grade) poly1 ] gbext integer
  [(isConstant) poly] gbext bool
  [(isConstantAll) poly] gbext bool
  [(isOrdered) poly] gbext poly
  [(isReducible) poly1 poly2 ] gbext integer
  [(lcm) poly1 poly2] gbext poly
  [(lcoeff) poly] gbext poly
  [(lmonom) poly] gbext poly
  [(mod) poly1 universalNumber] gbext poly
          poly = poly1 mod universalNumber where char=0 and
          poly and poly2 belong to a same ring.
  [(ord_ws_all) fv wv] gbext integer
  [(reduceContent) poly] gbext [poly c]
  [(tomodp) poly1 ring] gbext poly, char(ring)>0.
          poly = poly1 mod char(ring) where poly belongs to ring.
  [(tomod0) poly1 ring] gbext poly, char(ring)=0.
  [(schreyerSkelton) array_of_poly] gbext array
  [(toes) array_of_poly] gbext poly
  [(toe_) poly] gbext poly
  [(toe_) array_of_poly] gbext poly   cf. toVectors
```

1.29 get

```
<< [f0 f1 ... fn] k get fk >>
integer k;The primitive gets the k-th element of a given array.
Example: [1 4 3] 1 get :: ---> 4
<< ob [k0 k1 ... ] get f >>
It is equivalent to << ob k0 get k1 get ... >>
The primitive get works for array or list.
```

1.30 goto

```
<< label goto >>
literal label;
Break the loops and jump to the <<literal>>.
The label <<literal>> has to be out of all the loops.
You cannot jump inside of the executable array { .... }.
Example: /point goto (skip me) message /point
```

1.31 groebner

```
<< [[f1 ... fn] [options]] groebner
   [[g1 ... gm] backward-transformation syzygy]>>
poly f1, ..., fn; poly g1, ..., gm;
optional return value: matrix of poly backward-transformation, syzygy;
Computation of the Groebner basis of f1,...,fn. The basis is {g1,...,gm}.
Options: << (needBack), (needSyz), (reduceOnly), (gbCheck),
            (countDown) number (StopDegree) number, (forceReduction)>>
```

```
Flags:<< [(ReduceLowerTerms) 1] system_variable >>
      << [(AutoReduce) 0]         system_variable >>
      << [(UseCriterion1) 0]    system_variable >>
      << [(UseCriterion2B) 0]   system_variable >>
      << [(Sugar) 0]            system_variable >>
      << [(Homogenize) 1]       system_variable >>
      << [(CheckHomogenization) 1] system_variable >>
      << [(Statistics) 1]       system_variable >>
      << [(KanGBmessage) 1]     system_variable >>
      << [(Verbose) 0]          system_variable >>
Example: [(x0,x1) ring_of_polynomials 0] define_ring
         [(x0^2+x1^2-h^2). (x0 x1 -4 h^2).] /ff set ;
         [ff] groebner /gg set ;
         gg ::
cf. homogenize, groebner_sugar, define_ring,
    ring_of_polynomials, ring_of_differential_operators.
```

1.32 gt

```
<< o1 o2 lt r1  >> or  <<  o1 o2 gt r1 >> or <<  o1 o2 gt r1 >>
integer r1;
These premitives compare objects o1 and o2.
[lt (less than), gt (greater than), eq (equal)]
The result is r1 which is integer object.
Here, 1 means true and 0 means false.
Example:  (abc) (bca) eq ::  ===> 0
```

1.33 homogenize

```
<< f homogenize g >>
poly f,g;
array of poly f,g;

[(degreeShift) (value)] homogenize [shiftD shiftUV]
[(degreeShift) (reset)] homogenize [null null]
[(degreeShift) shiftD ] homogenize [shiftD shiftUV]
[(degreeShift) [shiftD shiftUV]] homogenize [shiftD shiftUV]
[(degreeShift) [ ]     fv] homogenize   hfv
[(degreeShift) shiftD  fv] homogenize   hfv
[(degreeShift) [shiftD shiftUV] fv] homogenize hfv
shiftD : degree shift vector for (0,1)-h homogenization
shiftUV : degree shift vector for (-1,1)-s homogenization (internal for ecart.)
fv : polynomial or vector of polynomials.
Example:  [(x) ring_of_differential_operators 0] define_ring
   [(degreeShift) [[1 0] [0 1]] [(x+1). (Dx+1).]] homogenize ::
   [(degreeShift) (value)] homogenize ::
Note. min of ord (-1,1)[0,1] is min {-1,1, 1+1,1+0} = -1 =m
      Degree of H is b-a+v(i)-m where v=[0,1]
Side effects:  It changes h-degree shift vector and s-degree shift vector
   in homogenizeObject_go(), which is called from ecart division codes
   as well as the function homogenize.
DegreeShift is automatically reset when set_up_ring is called.
```

1.34 idiv

```
<< a b idiv a/b >>
int a,b,a/b;
Example:  5 2 idiv ::  ===> 2
```

1.35 ifelse

```
<< condition { true case } { false case } ifelse >>
integer condition;
If condition is non-zero, then true-case will be executed,
else false-case will be executed.
```

1.36 index

```
<<  a_0 ... a_{n-1} n index a_0 ... a_{n-1} a_0 >>
integer n;
It takes a_0 from the stack.
```

1.37 init

```
<< f init h >>
<< f weight_vector init h >>
poly f,h; array of integer weight_vector;
h is the initial term of the polynomial f.
Example: (2 x^3 + 3 x + 1). init :: ---> 2 x^3
Example: [(x^3+1). (x h+ h^5).] {init} map ::
Example: (x+1). [0 1 1 1] init ::    cf. weightv

<< fv weight_vector init h >>
<< fv [weight_vector shift_vector] init h >>
<< fv init h >> or << hv [ ] init h >>
fv is a polynomial or a vector of polynomials.
h is the initial term with respect to the weight vector and the shift vector
if they are given.
Note: the last x variable is always assumed to be the vector index.
Example: [(x,y) ring_of_differential_operators 0] define_ring
    [(x^2*Dx^2+2*x*Dx+x). (Dx+x).] [[(Dx) 1 (x) -1] weightv [0 -1]] init ::
```

1.38 lc

```
<< obj lc leftCell >>
class leftCell;
```

```
leftCell is the left cell of the obj of which type must be class.
```

1.39 length

```
<< [a0 a1 ... an] length <n+1> >>
<< s length p >>
integer <n+1>; integer p; string s;
It returns the length of the argument. p is the length of the string.
```

1.40 load

```
<< /literal load obj >>
<<load>> gets the value of <<literal>>.
```

1.41 loop

```
<< {executable array} loop >>
cf. exit
```

1.42 lt

```
<< o1 o2 lt r1  >> or  <<  o1 o2 gt r1 >> or <<  o1 o2 gt r1 >>
integer r1;
These premitives compare objects o1 and o2.
[lt (less than), gt (greater than), eq (equal)]
The result is r1 which is integer object.
Here, 1 means true and 0 means false.
Example:  (abc) (bca) eq ::  ===> 0
```

1.43 map

```
<< [f1 ... fn] {code} map [f1 {code}exec ... fn {code}exec] >>
map applies {code} to each element in [f1 ... fn].
Example: [1 2 3] {1 add} map ===> [2 3 4]
```

1.44 mpzext

```
[(key) arguments] mpzext ans
It calls mpz functions.
arguments should be numbers(universalNumber).
Keys: gcd, tdiv_qr, cancel, powm, probab_prim_p, sqrt, and, ior, com
For details, see gmp-2.0.2/texinfo.tex.
```

1.45 mul

```
obj1 obj2 mul obj3
obj3 = obj1 * obj2
```

1.46 newcontext

```
<< name super newcontext class.Context >>
It creates new context and new user dictionary.
Ex. (mycontext) StandardContextp newcontext /nc set.
cf. setcontext.
```

1.47 newstack

```
<< size newstack class.OperandStack >>
cf. setstack, stdstack.
```

1.48 options

```
The keyword <<options>> cannot be found.
Type in ? in order to see system dictionary.
```

1.49 oxshell

```
<< cmds oxshell result >>
cmds is an array of strings.

command
Executing a command
cmdname arg1 arg2 ...
Example 1: /afo (Hello! ) def [(cat) (stringIn://afo)] oxshell
Example 2: [(polymake) (stringInOut://afo.poly) (FACETS)] oxshell
A temporary file afo.poly* with the contents of the variable afo.poly is generated under $TMP and "polymake $
Example 3: [(ls) (-l) (>) (stringOut://ff)] oxshell
command
export
export env_name  =  value
export env_name =
Example: [(export) (PATH) (=) (/usr/new/bin:${PATH})] oxshell
export
keep_tmp_files
keep_tmp_files value
If value is zero, then temporary files are removed after execution.
```

```
Example 1: [(keep_tmp_files) (1)] oxshell ; temporary files will be kept in /tmp or $TMP or ...
keep_tmp_files
killall
Kill all the processes envoked by oxshell
killall
redirect
The following redirect operators are implemented.
< > 2>
Example 1: [(ls) (hoge) (2>) (stringOut://afo)] oxshell
    afo ::
Example 2: [(cp) ] addStdoutStderr oxshell
      [@@@stdout @@@stderr] ::
redirect
which
which cmd_name
which cmd_name path
Example: [(which) (ls)] oxshell
which
```

1.50 pop

```
<< obj pop >>
It removes the obj from the stack.
```

1.51 primmsg

```
<< { executable array } primmsg >>
The << executable array >> is executed in the PrimitiveContext.
cf. sendmsg, sendmsg2, supmsg2, system_variable
```

1.52 principal

```
<< obj principal obj >>  Get the principal part.
This is an old command. init should be used.
Example: (x Dx + Dy^2+ y Dx Dy). [(Dx) 1 (Dy) 1] weightv init
```

1.53 print

```
<< obj print >>
Print the object to stdout. cf. obj (string) dc
```

1.54 print_switch_status

```
<< print_switch_status >>
```

```
cf. switch_function
```

1.55 pstack

```
<< pstack >>
The operator prints the entire contents of the stack.
```

1.56 pushfile

```
<< filename pushfile sss >>
string filename, sss ;
Read the file and push the contents of file as the string.
The file will be search in the search path as run operator.
Example: (myfile.txt) pushfile /sss set
cf:  [(parse) sss] extension
```

1.57 put

```
<< [a0 a1 ... ap] i any put >>
<< [a0 a1 ... ap] multi-index any put >>
<< s i any put >>
integer i; string s; array of integers multi-index;
The operator put <<any>> at the place i.
Example: /a [1 2 3] def  a 2 (Hi) put a :: --->[1 2 (Hi)]
Example: /a [[1 2] [3 4]] def  a [0 1] 10 put a :: --->
                                               [[1 10] [3 4]]
```

1.58 quit

```
The bye or QUIT or quit statement terminates the kan/sm1.
```

1.59 rc

```
<< obj rc rightCell >>
rightCell is the right cell of the obj of which type must be class.
class rightCell;
```

1.60 reduction

```
<< f [g_1 g_2 ... g_m] reduction [h c0 syz input] >>
poly f, g1_1, ..., g_m, h, c0; array of poly syz, input;
h is the normal of f by {g1 .... fm}.
```

```
h = c0 f + \sum syz_i g_i
```

1.61 replace

```
<< f [[L1 R1] ... [Ln Rn]] replace g >>
poly f, L1, R1, ..., Ln, Rn, g;
<<replace>> applies the rules L1-->R1, ..., Ln-->Rn to transform f.
Example: (x^2+x+1). [[(x). (2).]] replace :: ---> 7
```

1.62 roll

```
<< f(n-1) ... f(0) n j roll f(j-1 mod n) f(j-2 mod n) ... f(j-n mod n) >>
integer n, j;
Example: [(a) (b) (c) 3 1 roll] ::  ==>[(c) (a) (b)]
```

1.63 run

```
<< filename run >>
string filename ;
Example. (restriction.sm1) run
File will be searched in the current directory, /usr/local/lib/sm1,
and the directory specified by the environment variable LOAD_SM1_PATH
Example. setenv LOAD_SM1_PATH ~/lib/sm1/
```

1.64 sendmsg

```
<< obj { executable array } sendmsg >>
When obj is in k-class (i.e. obj is of the form
 [<<class.Context>> , body ]), then the CurrentContextp is changed
to <<class.Context>> and the obj <<executable array>> will be executed.
If not, CurrentContextp is changed to the PrimitiveContextp and
the obj <<executable array>> will be executed.
cf. setcontext, newcontext, StandardContextp, system_variable,
    sendmsg2, primmsg, supmsg2.
```

1.65 sendmsg2

```
<< obj2 obj3 { executable array } sendmsg2 >>
Context is determined by obj2 if obj2 is class.context.
If not, it is determined by obj3 if obj2 is class.context.
cf. sendmsg.
```

1.66 set

```
<< /name object def >>  or  << object /name set >>
The primitive def or set binds the object to the name
Example: /abc (23) def    abc :: ---> (23)
Example: (23) /abc set    abc :: ---> (23)
```

1.67 set_order_by_matrix

```
<< order-matrix set_order_by_matrix >>
matrix of integers order-matrix;
cf. weight_vector, show_ring, elimination_order, switch_function
    system_variable
```

1.68 set_timer

```
cf. timer
```

1.69 set_up_ring@

```
<< [x-variables] [d-variables] [p c l m n cc ll mm nn next] order-matrix
   [(keyword) value (keyword) value ....]  set_up_ring@ >>
<<next>> is the optional argument. The last argument is also optional.
Keywords are mpMult, coeffient ring, valuation, characteristic,
             schreyer, ringName.

1.When [x[0] .... x[n-1]] [D[0] .... D[n-1]] is given as the lists
  of variables, D[0] is usually used as the variable for homogenization
  and x[n-1] is used for the variable for the graduation.
2.Order matrix should be given in the order x[n-1] ... x[0], D[n-1]...D[0]
3.0<=i<c : commutative; c<=i<l : q-difference;
  l<=i<m : difference(better not to use it); m<=i<n : differential;
4.Graduation variables :
  cc<=i<c : commutative; ll<=i<l : q-difference;
  mm<=i<m : difference;  nn<=i<n : differential;
  If you do not use graduation variables, set, for example, cc=c.
5.c-cc>0 or l-ll>0 or m-mm>0 or n-nn>0 must be held.

Example: [$H$ $x$ $y$ $e$] [$h$ $Dx$ $Dy$ $E$]
         [0 1 1 1 4 1 1 1 3]
        (  e y x H   E Dy Dx h )
         [[1 1 1 1   1 1  1  0]
          [1 0 0 0   0 0  0  0]
          [0 0 0 0   0 1  0  0]
           ........

cf. polynomial_ring, ring_of_..., groebner.
```

1.70 setcontext

```
<< class.Context setcontext >>
Change the CurrentContextp (and the user dictionary) to class.Context.
Ex. (mynew) StandardContextp newcontext /cp set cp setcontext
cf. system_variable(CurrentContextp), newcontext,
    show_user_dictionary, StandardContextp.
```

1.71 setstack

```
<< class.OperandStack setstack >>
Change the current operand stack to class.OperandStack.
Ex. 1000 newstack /st set  st setstack
cf. newstack, stdstack
```

1.72 show_ring

```
<< show_ring >>
cf. set_up_ring.
```

1.73 show_systemdictionary

```
<< show_systemdictionary >>  << show_user_dictionary >>
```

1.74 show_user_dictionary

```
<< show_systemdictionary >>  << show_user_dictionary >>
```

1.75 spol

```
<< f  g spol  [ [c d] r] >>
poly f, g, c, d, r;
r is the s-polynomial of f and g.
 r = c f + d g
```

1.76 stdstack

```
<< stdstack >>
Change the current operand stack to the standard stack.
cf. newstack, setstack
```

1.77 sub

```
obj1 obj2 sub obj3
obj3 = obj1 - obj2.
```

1.78 supercontext

```
<< class.Context supercontext class.Context2 >>
cf. setcontext, newcontext
```

1.79 supmsg2

```
<< obj2 obj3 { executable array } supmsg2 >>
Context is the super of obj2 or obj3.
cf. sendmsg, sendmsg2, primmsg.
```

1.80 switch_function

```
<< (function) (name) switch_function >>
<< (report) (function) switch_function value >>
cf. print_switch_status, getOptions, restoreOptions.
```

1.81 system

```
<< command system >>
string command;
Execute unix command.
Example: (ls) system
```

1.82 system_variable

```
<< [(key word)] system_variable result >> or
<< [(key word) value] system_variable result >>
<< [(key word) optional arg] system_variable result >>
The primitive returns the value of a given system constant.
The primitive sets the value of a given system constant.
PrintDollar [0,1,2], Wrap, P, N, NN, M, MM, L, LL, C, CC,ringName,
CurrentRingp, Verbose, UseCriterion1, UseCriterion2B,
ReduceLowerTerms, CheckHomogenization, Homogenize, Sugar, Homogenize_vec,
Statistics, StackPointer, StandardOperandStack,
ErrorStack, ErrorMessageMode, WarningMessageMode,
CatchCtrlC, Strict, CurrentContextp, NullContextp, Strict2, QuoteMode
SigIgn, KSPushEnvMode, PrimitiveContextp, KanGBmessage,
orderMatrix, gbListTower, Schreyer,
```

```
outputOrder, multSymbol, variableNames, Version,
AvoidTheSameRing, RingStack, LeftBracket, RightBracket,
AutoReduce, Ecart, EcartAutomaticHomogenization
DoCancel, DebugContentReduction
RestrictedMode (cf. or_attr 8), SecureMode(obsolete)
UseDsmall, COutput
Example: [(N)] system_variable
                             (maximum number of variables)/2.
         [(x) (var) 3] system_variable
                              The 3rd variable.
         [(D) (var) 4] system_variable
                              The 4th differential operator.
         [(PrintDollar) 0] system_variable
                          Set the global variable PrintDollar to 0
DebugReductionEcart (bit):  (2) * (1) find_reducer,in(r)
              (any) cont   (4) #+[rat division, + ecartd]
                           (8) check the order.
DoCancel (bit):  (2) always_reduce_content  (1) Noro_strategy
                 (4) DoCancel_in_reduction1
```

1.83 test

```
The keyword <<test>> cannot be found.
Type in ? in order to see system dictionary.
```

1.84 tlimit

```
<< { ... } t tlimit results >>
Limit the execution time to t seconds.
When t is not positive, tlimit pushes the execution time.
```

1.85 to_records

```
<< ({arg1,arg2,...,argn})  to_records (arg1) ... (argn) n >>
Example: ({x,y2}) to_records ===> (x) (y2) 2
Example: (x,y2)   to_records ===> (x) (y2) 2
Example: [(x,y2) to_records pop] ===> [(x) (y2)]
cf. [(stringToArgv) str] extension or stringToArgv2
```

1.86 writestring

```
<< fd s writestring >>
file fd; string s;
Write the string s to the file fd.
cf. [(PrintDollar)] system_variable, file, closefile
```

2 Macro Operators

2.1

```
gate keeper
```

2.2 -intInfinity

```
-intInfinity = -999999999
```

2.3 .

```
string . polynomial
Parse the string as a polynomial in the current ring and put it on the stack
Example ( (x+2)^3 ) .
```

2.4 ..

```
 string .. universalNumber
Parse the << string >> as a universalNumber.
Example:  (123431232123123).. /n set
{ commands }..  executes the commands.  << .. >> is equivalent to exec.
```

2.5 ..int

```
universalNumber ..int int
```

2.6 ::

```
Pop the top of the stack and print it.
```

2.7 ;

```
Output the prompt sm1>
```

2.8 ==

```
obj ==
Print obj
```

2.9 @@@.Dsymbol

```
@@@. is the prefix for the global control variables and global functions.
@@@.quiet   :  1 ---> quiet mode,  0 ---> not. cf. sm1 -q
@@@.esymbol : (e_) is the standard value. It is used to express
              vectors internally. cf. fromVectors, toVectors
@@@.Dsymbol :  (D) is the standard value for differential operator.
                cf. ring_of_differential_operators
@@@.diffEsymbol :  (E) is the standard value for difference operator.
                cf. ring_of_difference_operators
@@@.Qsymbol :  (Q) is the standard value for q-difference operator.
                cf. ring_of_qdifference_operators
```

2.10 @@@.Qsymbol

```
@@@. is the prefix for the global control variables and global functions.
@@@.quiet   :  1 ---> quiet mode,  0 ---> not. cf. sm1 -q
@@@.esymbol : (e_) is the standard value. It is used to express
              vectors internally. cf. fromVectors, toVectors
@@@.Dsymbol :  (D) is the standard value for differential operator.
                cf. ring_of_differential_operators
@@@.diffEsymbol :  (E) is the standard value for difference operator.
                cf. ring_of_difference_operators
@@@.Qsymbol :  (Q) is the standard value for q-difference operator.
                cf. ring_of_qdifference_operators
```

2.11 @@@.diffEsymbol

```
@@@. is the prefix for the global control variables and global functions.
@@@.quiet   :  1 ---> quiet mode,  0 ---> not. cf. sm1 -q
@@@.esymbol : (e_) is the standard value. It is used to express
              vectors internally. cf. fromVectors, toVectors
@@@.Dsymbol :  (D) is the standard value for differential operator.
                cf. ring_of_differential_operators
@@@.diffEsymbol :  (E) is the standard value for difference operator.
                cf. ring_of_difference_operators
@@@.Qsymbol :  (Q) is the standard value for q-difference operator.
                cf. ring_of_qdifference_operators
```

2.12 @@@.esymbol

```
@@@. is the prefix for the global control variables and global functions.
@@@.quiet   :  1 ---> quiet mode,  0 ---> not. cf. sm1 -q
@@@.esymbol : (e_) is the standard value. It is used to express
              vectors internally. cf. fromVectors, toVectors
@@@.Dsymbol :  (D) is the standard value for differential operator.
                cf. ring_of_differential_operators
@@@.diffEsymbol :  (E) is the standard value for difference operator.
                cf. ring_of_difference_operators
@@@.Qsymbol :  (Q) is the standard value for q-difference operator.
                cf. ring_of_qdifference_operators
```

2.13 @@@.quiet

```
@@@. is the prefix for the global control variables and global functions.
@@@.quiet   :  1 ---> quiet mode,  0 ---> not. cf. sm1 -q
@@@.esymbol : (e_) is the standard value. It is used to express
             vectors internally. cf. fromVectors, toVectors
@@@.Dsymbol :  (D) is the standard value for differential operator.
               cf. ring_of_differential_operators
@@@.diffEsymbol :  (E) is the standard value for difference operator.
               cf. ring_of_difference_operators
@@@.Qsymbol :  (Q) is the standard value for q-difference operator.
               cf. ring_of_qdifference_operators
```

2.14 ArrayP

```
IntegerP, LiteralP, StringP, ExecutableArrayP, ArrayP, PolyP, FileP, RingP,
UniversalNumberP, RationalFunctionP, ClassP, DoubleP, ByteArrayP
      return data type identifiers.
Example:  7 tag IntegerP eq  ---> 1
```

2.15 ByteArrayP

```
IntegerP, LiteralP, StringP, ExecutableArrayP, ArrayP, PolyP, FileP, RingP,
UniversalNumberP, RationalFunctionP, ClassP, DoubleP, ByteArrayP
      return data type identifiers.
Example:  7 tag IntegerP eq  ---> 1
```

2.16 ClassP

```
IntegerP, LiteralP, StringP, ExecutableArrayP, ArrayP, PolyP, FileP, RingP,
UniversalNumberP, RationalFunctionP, ClassP, DoubleP, ByteArrayP
      return data type identifiers.
Example:  7 tag IntegerP eq  ---> 1
```

2.17 DoubleP

```
IntegerP, LiteralP, StringP, ExecutableArrayP, ArrayP, PolyP, FileP, RingP,
UniversalNumberP, RationalFunctionP, ClassP, DoubleP, ByteArrayP
      return data type identifiers.
Example:  7 tag IntegerP eq  ---> 1
```

2.18 ExecutableArrayP

```
IntegerP, LiteralP, StringP, ExecutableArrayP, ArrayP, PolyP, FileP, RingP,
UniversalNumberP, RationalFunctionP, ClassP, DoubleP, ByteArrayP
      return data type identifiers.
Example:  7 tag IntegerP eq  ---> 1
```

2.19 IntegerP

```
IntegerP, LiteralP, StringP, ExecutableArrayP, ArrayP, PolyP, FileP, RingP,
UniversalNumberP, RationalFunctionP, ClassP, DoubleP, ByteArrayP
      return data type identifiers.
Example:  7 tag IntegerP eq  ---> 1
```

2.20 Libraries

```
Doc/appell.sm1   : It generates Appell differential equations.
Doc/bfunction.sm1: Computing the b-function of a given polynomial
                   by using Groebner basis. Written by T.Oaku.
Doc/factor-a.sm1: A sample interface to factor polynomials by risa/asir.
Doc/gkz.sm1     : It generates GKZ systems for given A and b.
Doc/hol.sm1     : Basic package for holonomic systems. Holonomic rank,
                  characteristic ideal, singular locus.
Doc/resol0.sm1  : Constructing Schreyer resolutions. tower.sm1, tower-sugar.sm1
Doc/rest0.sm1   : Computing the restriction (inverse image) as a complex.
                  This package is under developement by T.Oaku.
                  cf. restall_s.sm1, resol0.sm1
```

2.21 LiteralP

```
IntegerP, LiteralP, StringP, ExecutableArrayP, ArrayP, PolyP, FileP, RingP,
UniversalNumberP, RationalFunctionP, ClassP, DoubleP, ByteArrayP
      return data type identifiers.
Example:  7 tag IntegerP eq  ---> 1
```

2.22 Loadall

```
Loadall loads the packages  bfunction.sm1, hol.sm1, gkz.sm1, appell.sm1,
resol0.sm1
```

2.23 PolyP

```
IntegerP, LiteralP, StringP, ExecutableArrayP, ArrayP, PolyP, FileP, RingP,
UniversalNumberP, RationalFunctionP, ClassP, DoubleP, ByteArrayP
      return data type identifiers.
Example:  7 tag IntegerP eq  ---> 1
```

2.24 RationalFunctionP

```
IntegerP, LiteralP, StringP, ExecutableArrayP, ArrayP, PolyP, FileP, RingP,
UniversalNumberP, RationalFunctionP, ClassP, DoubleP, ByteArrayP
      return data type identifiers.
Example:  7 tag IntegerP eq  ---> 1
```

2.25 RingP

```
IntegerP, LiteralP, StringP, ExecutableArrayP, ArrayP, PolyP, FileP, RingP,
UniversalNumberP, RationalFunctionP, ClassP, DoubleP, ByteArrayP
      return data type identifiers.
Example:  7 tag IntegerP eq  ---> 1
```

2.26 SmallRing

```
SmallRing is the ring of polynomials Q[t,x,T,h].
```

2.27 StringP

```
IntegerP, LiteralP, StringP, ExecutableArrayP, ArrayP, PolyP, FileP, RingP,
UniversalNumberP, RationalFunctionP, ClassP, DoubleP, ByteArrayP
      return data type identifiers.
Example:  7 tag IntegerP eq  ---> 1
```

2.28 UniversalNumberP

```
IntegerP, LiteralP, StringP, ExecutableArrayP, ArrayP, PolyP, FileP, RingP,
UniversalNumberP, RationalFunctionP, ClassP, DoubleP, ByteArrayP
      return data type identifiers.
Example:  7 tag IntegerP eq  ---> 1
```

2.29 Version

```
Packages must be loaded in a proper version of kan/sm1.
It can be checked as follows.
Example:
   /factor-a.version (2.981101) def
   factor-a.version [(Version)] system_variable gt
   { (This package requires the latest version of kan/sm1) message
     (Please get it from http://www.math.kobe-u.ac.jp/KAN) message
     error
   } { } ifelse
```

2.30 __

```
 string ring __ polynomial
Parse the <<string>> as an element in the <<ring>> and returns
the polynomial.
cf. define_ring, define_qring, ring_def
Example: [(x,y) ring_of_polynomials [[(x) 1]] weight_vector 7]define_ring
         /myring set
         ((x+y)^4) myring __ /f set
```

2.31 ___

```
reparse a polynomial or polynomials
```

2.32 action

```
 f g action p
<poly> f,g,p
Act f on g. The result is p. The homogenization variable h is put to 1.
We can use diff0 only in the ring of differential operators.
Example: [(x) ring_of_differential_operators 0] define_ring
         (Dx^2). (x^2). action ::
```

2.33 adjoint

```
f xlist adjoint g
poly f; string xlist; poly g;
g is the adjoint operator of f.
The variables to take adjoint are specified by xlist.
Example: [(x,y) ring_of_differential_operators 0] define_ring
          (x^2 Dx - y x Dx Dy-2). (x,y) adjoint
          ((-Dx) x^2 - (-Dx) (-Dy) x y -2). dehomogenize sub :: ==> 0
```

2.34 and

```
obj1 obj2 and bool
```

2.35 append

```
list1 obj2 append list3
Ex.  [1 2]  3 append  [1 2 3]
```

2.36 arrayToList

```
a arrayToList list
```

2.37 beginEcart

```
beginEcart
Set the environments for the ecart division algorithm.
```

2.38 boundp

```
 a boundp b
string a, b is 0 or 1.
If the variable named << a >> is bounded to a value,
```

it returns 1 else it returns 0.
Example: (hoge) boundp ::

2.39 break

bool break

2.40 bugs

All known bugs are fixed.

2.41 cancel

obj cancel r
Cancel numerators and denominators
The implementation has not yet been completed. It works only for Q.

2.42 cancelCoeff

f cancelcoeff g
poly f,g;
Factor out the gcd of the coefficients.
Example: (6 x^2 - 10 x). cancelCoeff
See also gbext.

2.43 carN

[f1 ... fm] n carN [f1 ... fn]
carN extracts the first n elements from the list.

2.44 cat

a cat s
array a ; string s;
cat converts each entry of << a >> to a string and concatenates them.
Example: [(x) 1 2] cat ==> (x12)

2.45 complement

set universal_set complement complement_set
Example: [1 2] [3 4 1 2 5] complement ::

2.46 cons

```
obj list cons list
```

2.47 ctrlC-hook

```
When ctrl-C is pressed, this function is executed.
User can define one's own ctrlC-hook function.
```

2.48 dc

```
Abbreviation of data_conversion.
```

2.49 define_qring

```
 [varlist ring_of_q_difference_operators order characteristic] define_qring
    Pointer to the ring.
Example: [$x,y$ ring_of_q_difference_operators $Qx,Qy$ elimination_order
          0] define_qring
cf. define_ring, set_up_ring@ <coefficient ring>, ring_def, << __ >>
```

2.50 define_ring

```
 [varlist ring_of_??? order characteristic options] define_ring
 Pointer to the ring.
Example: [(x,y,z) ring_of_polynomials [[(x) 100 (y) 10 (z) 1]] weight_vector
          11] define_qring
Example: [(x,y) ring_of_polynomials [[(x) 1]] weight_vector 0 ] define_ring
         /R set
cf. define_qring, set_up_ring@ <coefficient ring>
    <<ring_of_???>> ring_of_polynomials, ring_of_differential_operators,
    ring_of_difference_operators
    <<order>> elimination_order, weight_vector
    ring_def,ring , << __ >>
```

2.51 define_ring_variables

```
It binds  a variable <<a>> in the current ring to the sm1 variable <<a>>.
For example, if x is a variable in the current ring, it defines the sm1
variable x by /x (x) def
```

2.52 dehomogenize

```
obj dehomogenize obj2
dehomogenize puts the homogenization variable to 1.
Example:  (x*h+h^2). dehomogenize ::    x+1
```

2.53 denominator

```
[a b c ...] denominator r
 a denominator r
cf. dc, numerator
Output is Z or a polynomial.
```

2.54 diff0

```
f v n diff0 fn
<poly> fn, v ; <integer>  n ; <poly> fn
fn = v^n f where v^n is the operator to take the n-th differential.
We can use diff0 only in the ring of differential operators.
Example: [(x) ring_of_differential_operators 0] define_ring
         (x^10-x). (Dx). 1 diff0 ::
```

2.55 distraction

```
f [ list of x-variables ] [ list of D-variables ] [ list of s-variables ]
   distraction  result
Example: (x Dx Dy + Dy). [(x). (y).] [(Dx). (Dy).] [(x). (y).] distraction
```

2.56 distraction2

```
f [ list of x-variables ] [ list of D-variables ] [ list of s-variables ]
   distraction2  result
Example 1: [(x,y) ring_of_differential_operators 0] define_ring
  (x^2 Dx Dy + x Dy). [(x). (y).] [(Dx). (Dy).] [(x). (y).] distraction2
Example 2: (x^4 Dx^2 + x^2). [(x).] [(Dx). ] [(x).] distraction2
```

2.57 doPolymake

```
It calls polymake via oxshell and ox_k0 to make several construction for polytopes.
[action data_in_polymake_tfb_format] doPolymake
        [result_in_tfb result_in_tree errors]
polymake, polymake2tfb, ox_k0 must be installed.
cf. @@@polymake.k0.ccc, kan96xx/Doc/oxshell.*, kan96xx/trans/polymake.sm1, oxshell
The variable @@@doPolymake.vars keeps session logs with the polymake
See also usePolymake.local, usePolymake.OoHG.native and usePolymake.OoHG.curl in cgi.sm1
Example:
 usePolymake.OoHG.curl polymake.start ;
 [(FACETS) (polymake.data(polymake.POINTS([[1,0,0],[1,1,0],[1,0,1],[1,1,1/2]])))]
        doPolymake /rr set
 Keys---properties are FACETS, CONE_DIM, LINEARITY_DIM, FEASIBLE, AFFINE_FULL, ...
```

2.58 eliminatev

```
[g1 g2 g3 ...gm] [list of variables] eliminatev [r1 ... rp]
Example: [(x y z - 1). (z-1). (y-1).] [(x) (y)] eliminatev [ z-1 ]
```

2.59 endEcart

```
endEcart
End of using the ecart division algorithm.
```

2.60 etag

```
obj etag integer
etag returns extended object tag. cf. kclass.c
```

2.61 evecw

```
size position weight evecw  [0 0 ... 0 weight 0 ... 0]
Example: 3 0 113 evecw ===> [113  0  0]
```

2.62 evenQ

```
number evenQ bool
```

2.63 execve

```
command execve
[arg0 arg1 arg2 ...] execve
It executes the command by the system call execve.
cf. system, forkExec
```

2.64 extension-examples

```
putAttributeList
  [(putAttributeList) [[(x+y-1) (x-y-2)] (x,y)]
                      [(needSyz) 1 (sugar) 1]] extension /myarg set
  [(getAttributeList) myarg] extension ::
  [(getAttribute) myarg (sugar)] extension ::
```

2.65 extension-treeToPolymake

```
$polymake.data(polymake.POINTS([[1,0,0],[1,1,0],[1,0,1],[1,1,1],[1,2,0]]),polymake.FACETS([[1,0,-1],[0,1,0],[
[(parse) (ox.sm1) pushfile] extension
k0connectr
oxk0.ccc ( polymake=Object; ) oxexecutestring
oxk0.ccc ( QuoteMode(1); ) oxexecutestring
oxk0.ccc pstr oxexecutestring
oxk0.ccc oxpopcmo /ptree set
oxk0.ccc ( QuoteMode(0); ) oxexecutestring
[(treeToPolymake) ptree] extension /ss set
ss message
```

2.66 factor

```
Load Doc/factor-a.sm1, then factorization can be computed by invoking
asir, of which ftp cite is at http://www.math.kobe-u.ac.jp
```

2.67 factorial

```
f n factorial g
integer n,  g is f (f-1) ... (f-n+1)
```

2.68 findIntegralRoots

```
 f findIntegralRoots vlist
poly f; list of integers vlist;
string f; list of integers vlist;
f is a polynomials in one variable s. vlist the list of integral roots sorted.
Example: (s^4-1) findIntegralRoots
```

2.69 flatten

```
list flatten list2
Flatten the list.
Example 1: [ [1 2 3] 4 [2]] flatten    ===> [1 2 3 4 2]
```

2.70 fromVectors

```
[v1 v2 ...] fromVectors [s1 s2 ...]
array of poly : v1, v2, ... ; poly : s1, s2 ....
cf. toVectors. <<e_>> varaible is assumed to be the last
    variable in x.  @@@.esymbol
Example: [(x,y) ring_of_differential_operators 0] define_ring
 [(x).  (y).] /ff set
 [ff ff] fromVectors ::
```

2.71 from_records

```
[s1 s2 s3 ... sn] from_records (s1,s2,...,sn,)
Example : [(x) (y)] from_records ::    (x,y,)
cf. to_records
```

2.72 gcd

```
[a b c ...] gcd r
cf. polygcd, mpzext
```

2.73 ge

```
obj1 obj2 ge bool
greater than or equal
```

2.74 gensym

```
x i gensym xi
string x; integer i; string xi
It generate a string x indexed with the number i.
Example:  (Dx) 12 gensym (Dx12)
```

2.75 getAttribute

```
ob key getAttribute value
Example: [(x-1) (y-1)] (gb) 1 setAttribute /ff set
         ff (gb) getAttribute ::
```

2.76 getAttributeList

```
ob getAttributeList attr-obj
Example: [(x-1) (y-1)] [(gb) 1] setAttributeList /ff set
         ff getAttributeList ::
```

2.77 getFileType

```
string getFileType type
Example: (/www/prog/cohom.sm1) getFileType ==> (sm1)
```

2.78 getNode

```
ob key getNode node-value
ob is a class object or an array.
The operator getNode returns the node with the key in ob.
When ob is a class, the node is an array of the format [key attr-list node-list]
When ob is an array, the node is a value of key-value pairs.
Example:
  /dog [(dog) [[(legs) 4] ] [ ]] [(class) (tree)] dc def
  /man [(man) [[(legs) 2] ] [ ]] [(class) (tree)] dc def
  /ma [(mammal) [ ] [man dog]] [(class) (tree)] dc def
  ma (dog) getNode
Example 2:
 [ [1 ] [2 3] [[(dog) 2]]] (dog) getNode ::
```

2.79 getOptions

```
 getOptions [<options for system_variable>  <options for switch_function>]
cf. restoreOptions
```

2.80 getOrderMatrix

```
obj getOrderMatrix m
array  m
getOrderMatrix obtains the order matrix from obj.
If obj is a polynomial, it returns the order matrix associated to
the polynomial.
If obj is an array, it returns an order matrix of an element.
```

2.81 getRing

```
obj getRing rr
ring rr;
getRing obtains the ring structure from obj.
If obj is a polynomial, it returns the ring structure associated to
the polynomial.
If obj is an array, it recursively looks for the ring structure.
cf. ring_def
```

2.82 getVariableNames

```
getVariableNames list-of-variables
Example: getVariableNames :: [e,x,y,E,H,Dx,Dy,h]
```

2.83 getvNames

```
getvNames vlist
list vlist
It returns of the list of the variables in the order x0, x1, ..., D0, ...
Use with [(variableNames) vlist] system_variable.
cf. nlist getvNames0 vlist is used internally. cf. getvNamesC
```

2.84 getvNamesC

```
getvNamesC vlist
list vlist
It returns of the list of the variables in the order 0, 1, 2, ...
(cmo-order and output_order).
cf. getvNames
```

2.85 getvNamesCR

```
obj getvNamesCR vlist
obj ring | poly ; list vlist
It returns of the list of the variables in the order 0, 1, 2, ... (cmo-order)
for <<obj>>.
Example: ( (x-2)^3 ). /ff set
```

```
[(x) ring_of_differential_operators 0] define_ring ff getvNamesCR ::
```

2.86 groebner_sugar

```
groebner_sugar computes Groebner basis by the sugar strategy.
Format of arguments and results are as same as that of groebner.
See groebner.  When you compute in the ring of polynomials,
it is recommended to turn on the switch [(UseCriterion1) 1] system_variable
Note that groebner_sugar does not use the homogenized Weyl algebra.
So, it does work only for term orders. Never use negative weight vectors.
```

2.87 hilb

```
base vlist hilb f
array of poly base; array of poly vlist;  poly f;
array of string base; array of string vlist; poly f;
array of string base; string vlist; number m; poly f;
f is the hilbert function (a_d x^d + ...)/m!
The << base >> should be a reduced Grobner basis.
Or, when the << base >> is an array of string,
all entries should be monomials.
Example: [(x^2) (x y )] (x,y)  hilb ::   h + 2
Example: [(x^2) (y^2)] (x,y) hilb  4
Example: [(x^2) (y^2) (x y)] [(x) (y)] hilb ::  3
cf. hilbert,    hilbReduce
```

2.88 hilbReduce

```
[f,g] v hilbReduce p
output of hilbert [f,g];  string v; poly p
p is  (g/(f!))*deg(g)!
 [(x) (y^3)] (x,y,z) hilbert (h) hilbReduce
```

2.89 hilbert

```
base vlist hilbert [m f]
array of poly base; array of poly vlist; number m; poly f;
array of string base; array of string vlist; number m; poly f;
array of string base; string vlist; number m; poly f;
[m f] represents the hilbert function (a_d x^d + ...)/m! where f=a_d x^d + ...
The << base >> should be a reduced Grobner basis.
Or, when the << base >> is an array of string,
all entries should be monomials.
Example: [(x^2) (x y )] (x,y)  hilbert ::  [2, 2 h + 4]
Example: [(x^2) (y^2)] (x,y) hilbert (h) hilbReduce ::  4
Example: [(x^2) (y^2) (x y)] [(x) (y)] hilbert (h) hilbReduce ::  3
cf. hilb,    hilbReduce
```

2.90 intInfinity

```
intInfinity = 999999999
```

2.91 ip1

```
 [v1 ... vn] [w1 ... wn] m ip1 [f1 ... fs]
<poly> v1 ... vn ; <integer> w1 ... wn m
<poly> f1 ... fs
Example: [(x,y) ring_of_differential_operators 0] define_ring
         [(Dx). (Dy).] [2 1] 3 ip1  ::    [(2 Dx Dy). (Dy^3).]
         Returns Dx^p Dy^q such that  2 p + 1 q = 3.
```

2.92 isArray

```
obj isArray bool
```

2.93 isByteArray

```
obj isByteArray bool
```

2.94 isClass

```
obj isClass bool
```

2.95 isDouble

```
obj isDouble bool
```

2.96 isInteger

```
obj isInteger bool
```

2.97 isPolynomial

```
obj isPolynomial bool
```

2.98 isRational

```
obj isRational bool
```

2.99 isRing

```
obj isRing bool
```

2.100 isString

```
obj isString bool
```

2.101 isSubstr

```
s1 s2 isSubstr pos
If s1 is a substring of s2, isSubstr returns the position in s2 from which
s1 is contained in s2.
If s1 is not a substring of s2, then isSubstr returns -1.
```

2.102 isUniversalNumber

```
obj isUniversalNumber bool
```

2.103 join

```
list1 list2 join list3
Ex.  [1 2] [3 [4 (ab)]] join  [1 2 3 [4 (ab)]]
Note: Join should use for arrays. It works for list too,
      but it does not copy cells. cf. cons
      So, it might generate looped lists or destroy other lists.
```

2.104 laplace0

```
f [v1 ... vn] laplace0 g
poly f ; string v1 ... vn ; poly g;
array of poly f ; string v1 ... vn ; array of poly g;
 g is the lapalce transform of f with respect to variables v1, ..., vn.
Example: (x Dx + y Dy + z Dz). [(x) (y) (Dx) (Dy)] laplace0
 x --> -Dx, Dx --> x,  y --> -Dy, Dy --> y.
```

2.105 lcm

```
[a b c ...] lcm r
cf. polylcm, mpzext
```

2.106 le

```
obj1 obj2 le bool
less than or equal
```

2.107 listToArray

```
list listToArray a
```

2.108 localizedString

```
string localizedString translatedString
It returns localizedString if localizedString.dic [array] and
localizedString.local [function] are set.
```

2.109 makeInfix

```
literal makeInfix
Change literal to an infix operator.
Example: /+ { add } def
  /+ makeInfix
  /s 0 def 1 1 100 { /i set s + i /s set } for s message
  [ 1 2 3 ] { /i set i + 2 } map ::
```

2.110 makeRingMap

```
 rule  ring1 ring2 makeRingMap maptable
makeRingMap is an auxiliary function for the macro ringmap. See ringmap
```

2.111 maxInArray

```
 [v1 v2 ....] maxInArray m
m is the maximum in [v1 v2 ...].
The position of m is stored in the global variable maxInArray.pos.
```

2.112 memberQ

```
element array(list) memberQ bool
```

2.113 message

```
string message
Output the string to the screen with the newline.
cf. messagen.
Example:  (Hello world) message
```

2.114 message-quiet

```
s message-quiet
string s;
It outputs the message s when @@@.quiet is not equal to 1.
```

@@@.quiet is set to 1 when you start sm1 with the option -q.

2.115 messagen

string messagen
Output the string to the screen without the newline.
cf. message.
Example: (Hello world) messagen

2.116 messagen-quiet

s messagen-quiet
string s;
It outputs the message s without the newline when @@@.quiet is not equal to 1.
@@@.quiet is set to 1 when you start sm1 with the option -q.

2.117 newMatrix

[m n] newMatrix mat

2.118 newVector

n newVector vec

2.119 ngcd

nlist ngcd d
list of numbers nlist; number d;
d is the gcd of the numbers in nlist.
Example: [(12345).. (67890).. (98765)..] ngcd

2.120 nl

nl is the newline character.
Example: [(You can break line) nl (here.)] cat message

2.121 nnormalize_vec

pp nnormalize_vec npp
It normalizes a given vector of Q into a vector of Z with relatively prime
entries by multiplying a postive number.

2.122 not

```
int not int
1 not 0
0 not 1
```

2.123 note-class

```
Example 1: [(object) [ ] [1,2]] [(class) (tree)] dc /ff set
           ff (array) dc ::
cf. data_conversion, kan96xx/Kan/kclass.c (KclassDataConversion)
```

2.124 npower

```
obj1 obj2 npower obj3
npower returns obj1^obj2 as obj3
The difference between power and npower occurs when we compute f^0
where f is a polynomial.
power returns number(universalNumber) 1, but npower returns 1
in the current ring.
```

2.125 null

```
<<null>> returns null object
```

2.126 numerator

```
[a b c ...] numerator r
 a numerator r
cf. dc, denominator
Output is a list of Z or polynomials.
```

2.127 or

```
obj1 obj2 or bool
```

2.128 ord_w

```
ff [v1 w1 v2 w2 ... vm wm] ord_w d
poly ff; string v1; integer w1; ...
order of the initial of ff by the weight vector [w1 w2 ...]
Example: [(x,y) ring_of_polynomials 0] define_ring
         (x^2 y^3-x). [(x) 2 (y) 1] ord_w ::
```

2.129 ord_w_all

```
ff [v1 w1 v2 w2 ... vm wm] ord_w d
poly ff; string v1; integer w1; ...
order of ff by the weight vector [w1 w2 ...]
Example: [(x,y,t) ring_of_polynomials 0] define_ring
          (x^2 y^3-x-t). [(t) 1 ] ord_w_all ::
```

2.130 ord_ws_all

```
fv wv ord_ws_all degree
  ord_ws_all returns the ord with respect to the weight vector wv.
Example: [(x,y) ring_of_differential_operators 0] define_ring
        (Dx^2+x*Dx*Dy+2). [(Dx) 1 (Dy) 1] weightv ord_ws_all ::

fv [wv shiftv] ord_ws_all degree
  ord_ws_all returns the ord with respect to the weight vector wv and
  the shift vector shiftv.
Example: [(x,y) ring_of_differential_operators 0] define_ring
        [(Dx^2+x*Dx*Dy+2). (Dx).] [[(Dx) 1 (Dy) 1] weightv [0 2]] ord_ws_all ::

cf: init, gbext.   Obsolete: ord_w, ord_w_all
```

2.131 output

```
obj output
Output the object to the standard file sm1out.txt
```

2.132 output_order

```
 [(v1) (v2) ...] output_order
Set the order of variables to print for the current ring.
cf. system_variable
Example:  [(y) (x)] output_order
           (x*y). ::   ===> y*x
```

2.133 oxasir

```
ox_asir is an asir server which is complient to open xxx protocol.
This module is necessary for efficient execution factorization
of b-functions in annfs, deRham.  cf. lib/oxasir.sm1
ox_asir has not yet been put on the ftp cite. 12/17, 1998.
```

2.134 plugin-cmo

```
Cmo extension is for supporting OpenXM cmo data.
See http://www.openxm.org for the latest info.
cmoObjectToCmo obj, cmoDumpCmo cmo-obj, cmoCmoToObject cmo-obj,
cmoCmoToStream cmo-obj stream, cmoStreamToCmo stream, cmoToStream stream,
cmoFromStrem stream, cmoMathCap,
```

```
cmoDebugCMO inteter,  cf. ox, plugin-ox, oxPrintMessage
cmoOxSystem, cmoOxSystemVersion, cmoLispLike
Example 1: [(cmoObjectToCmo) 3] extension /ff set ;
           [(cmoDumpCmo) ff] extension ;
Example 2: (t.t) (w) file /fd set ;
           [(cmoObjectToCmo) 3] extension /ff set ;
           [(cmoCmoToStream) ff fd] extension ;
           fd closefile ;
Example 3: Execute the following command on ox_sm1
           [(cmoLispLike) 1] extension
           then the received cmo data will be displayed on the server window.
```

2.135 plugin-file2

```
[(fp2clearReadBuf) file-fp2] extension c
[(fp2dumpBuffer) file-fp2] extension c
[(fp2fdopen) fd-num] extension file-fp2
[(fp2fflush) file-fp2] extension result
[(fp2fclose) file-fp2] extension result. fp2close is used for pclose, too.
[(fp2fgetc) file-fp2] extension c
[(fp2fileno) file-fp2] extension fd
[(fp2fopen) name mode] extension file-fp2
[(fp2fputc) c file-fp2] extension c
[(fp2mkfifo) name] extension status
[(fp2openForRead) name] extension fd-num
[(fp2openForWrite) name] extension fd-num
[(fp2popen) name mode] extension file-fp2
[(fp2pushfile) name] extension array-of-int
[(fp2select) file-fp2 t] extension status
```

2.136 plugin-ox

```
OX is for supporting Open XM communication protocol.
See http://www.math.kobe-u.ac.jp/OpenXM for the latest info.
This document is incomplete. See lib/ox.sm1 and plugin-cmo.
oxCreateClient, oxCreateClientFile, oxReq, oxGet, oxGetFromControl,
oxMultiSelect, oxWatch, oxCloseClient, oxSerial, oxGenPortFile,
oxRemovePortFile, oxGenPass, oxGetPort, oxCreateClient2,
oxPrintMessage cf. plugin-cmo, cmoDebugCMO
oxGetClientList
```

2.137 plugin-sm1.socket

```
[(sm1.socket) key [args] ] extension result-object
 key  :  open, connect, accept, select, mselect, read, write, readByte, writeByte, close.
Note that read and write are used for only string data.
See also Kan/debug/server.sm1

 (open) [portNumber hostname]  ---> [fd0 portNumber]
 (accept) [fd0]                ---> fd
 (connect) [portNumber hostname] -> [fd portNumber]
 (select) [fd time]            ---> 1 (ready) or 0
     if (time < 0) then it waits until data comes.
```

```
(mselect) [[fd0 fd1 ... ] time] -> [s0 s1 s2 ... ]
(read) [fd]                    ---> string-obj
(write) [fd string-obj]        ---> n-of-bytes-written
(readByte) [fd]                ---> data(byte)
(writeByte) [fd data(byte)]    ---> n-of-bytes-written
(writeByte) [fd array_of_data]---> n-of-bytes-written
(close) [fd]                   ---> status
```

2.138 pmat

```
f pmat
array f;
f is pretty printed.
```

2.139 popEnv

```
envlist popEnv
cf. pushEnv
```

2.140 position

```
set element position number
Example: [(cat) (dog) (hot chocolate)] (cat) position ===> 0.
```

2.141 power

```
obj1 obj2 power obj3
obj3 is (obj1)^(obj2). cf. npower
Example:  (2). 8 power ::  ===>  256
```

2.142 pushEnv

```
keylist pushEnv envlist
array of string keylist, array of [string object] envlist;
Values <<envlist>> of the global system variables specified
by the <<keylist>> is push on the stack.
keylist is an array of keywords for system_variable.
cf. system_variable, popEnv
Example:  [(CurrentRingp) (KanGBmessage)] pushEnv
```

2.143 pushVariables

```
varlist pushVariables pushed-variables
The macro is used to define local variables in a macro.
Example : /foo {
           /arg1 set
          [/abc /cd] pushVariables
          [ /abc arg1 def
```

```
          /cd abc 1 add def
          /arg1 cd def
        ] pop
        popVariables
        arg1
        } def
10 foo ::    returns 11
  In the example, abc and cd are local variables.
```

2.144 putUsages

```
[(key word) [(explanation line 1) (explanation line 2) ... ]] putUsages
```

2.145 reducedBase

```
base reducedBase reducedBase
<<reducedBase>> prunes redundant elements in the Grobner basis <<base>> and
returns <<reducedBase>>.
Ex. [(x^2+1). (x+1). (x^3).] reducedBase ---> [(x+1).]
```

2.146 reduction-noH

```
f g reduction-noH r
poly f; array g; array r;
Apply the normal form algorithm for f with the set g. All computations are
done with the rule Dx x = x Dx +1, i.e., no homogenization, but other
specifications are the same with reduction. cf. reduction
g should be dehomogenized.
```

2.147 rest

```
array rest the-rest-of-the-array
Ex. [1 2 [3 0]] rest ===> [2 [3 0]]
```

2.148 restoreOptions

```
[<options for system_variable>  <options for switch_function>] restoreOptions
cf. getOptions
```

2.149 reverse

```
array reverse reversed_array
```

2.150 ring_def

```
ring ring_def
Set the current ring to the <<ring>>
Example: [(x,y) ring_of_polynomials [[(x) 1]] weight_vector 0 ] define_ring
          /R set
          R ring_def
In order to get the ring object R to which a given polynomial f belongs,
one may use the command
          f (ring) data_conversion /R set
cf. define_ring, define_qring, system_variable, poly (ring) data_conversion
cf. << __ >>, getRing
```

2.151 ring_of_difference_operators

```
string ring_of_difference_operators
!!! OBSOLETE !!!

This command has not been maintained since 1996. So, there may be
troubles if it is used with new features of kan/sm1.

This command is used to define a ring of difference operators
with the macros define_ring, weight_vector and elimination_order.
The user cannot use the variable names h, e, H and E.
cf. show_ring, system_variable --- CurrentRing
    print_switch_status, switch_function
Example: [(x,y,z) ring_of_difference_operators (Ex,Ey) elimination_order 0] define_ring
         Ex,Ey, and Ez are corresponding difference operators to the
         space variables x, y and z ( Ex x = (x+1) Ex).
```

2.152 ring_of_differential_difference_operators

```
[string1 string2]  ring_of_differential_difference operators
This command is used to define a ring of differential-difference operators
with the macros define_ring, weight_vector and elimination_order.
string1 is a set of variables for differential operators.
string2 is a set of variables for difference operators.
The user cannot use the variable names h, e, H and E.
cf. show_ring, system_variable --- CurrentRing
    print_switch_status, switch_function
Example: [[(x,y) (s)] ring_of_differential_difference_operators
          [[(Es) 1] [(s) 1]] weight_vector 0] define_ring
         Dx and Dy are corresponding differential operators to the
         space variables x and y.  Try show_ring to see the commutation
         relations.
Example: contiguity of 1F1. Eb b = (b-1) Eb
 [ [(x) (a,b)] ring_of_differential_difference_operators
  [[(Dx) 1]] weight_vector 0] define_ring
 [ ( x Dx (x Dx+b-1) -x (x Dx+a) ).
 ( (x Dx +b-1) - (b-1) Eb ). ] /ff set
 ff {dehomogenize homogenize} map /ff2 set
 [ff2] groebner /gg set
 gg dehomogenize 0 get /gg set
 gg [(Dx)] eliminatev /gg2 set
 gg2 pmat
```

2.153 ring_of_differential_operators

```
string ring_of_differential_operators
This command is used to define a ring of differential operators
with the macros define_ring, weight_vector and elimination_order.
The user cannot use the variable names h, e, H and E.
cf. show_ring, system_variable --- CurrentRing
    print_switch_status, switch_function
Example: [(x,y) ring_of_differential_operators [[(Dx) 1 (Dy) 1]]
           weight_vector 0] define_ring
   Define the ring of differential operators Q<x,y,Dx,Dy> with the order
   obtained by refining the partial order defined by the weight vector
   [x,y,Dx,Dy] = [0,0,1,1]
Example: [(x,y) ring_of_differential_operators 0 [(weightedHomogenization) 1]]
          define_ring
Example: [(x,y) ring_of_differential_operators [[(x) -1 (Dx) 1]] weight_vector
          0 [(degreeShift) [[1 0 1]]] ]
          define_ring
Example: [(x,y,z) ring_of_differential_operators (Dx,Dy) elimination_order 0] define_ring
         Dx,Dy, and Dz are corresponding differential operators to the
         space variables x, y and z.
```

2.154 ring_of_polynomials

```
string ring_of_polynomials
This command is used to define a ring of polynomials with the macros
define_ring, weight_vector and elimination_order.
The user cannot use the variable names h, e, H and E.
cf. show_ring, system_variable --- CurrentRing
    print_switch_status, switch_function
Example: [(x,y,z) ring_of_polynomials (x,y) elimination_order 0] define_ring
```

2.155 ring_of_q_difference_operators

```
string ring_of_q_difference_operators

This command has not been maintained since 1996. So, there may be
troubles if it is used with new features of kan/sm1.

This command is used to define a ring of q-difference operators
with the macros define_qring, weight_vector and elimination_order.
Note that you should use this macro with define_qring instead of
define_ring.
The user cannot use the variable names h, e, q and E.
cf. show_ring, system_variable --- CurrentRing
    print_switch_status, switch_function
Example: [(x,y,z) ring_of_q_difference_operators (Qx,Qy) elimination_order 0] define_qring
         Qx,Qy, and Qz are corresponding q-difference operators to the
         space variables x, y and z ( Qx x = (q) x Q).
```

2.156 ringmap

```
f mapTable ringmap r
f is mapped to r where the map is defined by the mapTable, which is generated
by makeRingMap as follows:
 rule  ring1 ring2 makeRingMap maptable
Example:
[(x,y) ring_of_differential_operators ( ) elimination_order 0] define_ring
/R1 set
[(t,y,z) ring_of_differential_operators ( ) elimination_order 0] define_ring
/R2 set
[[(x) (Dx)] [((t-1) Dt) (z)]] /r0 set
r0 R1 R2 makeRingMap /maptable set
(Dx-1) R1 __ /ff set
 ff maptable ringmap ::
```

2.157 setAttribute

```
ob key value setAttribute new-obj
Example: [(x-1) (y-1)] (gb) 1 setAttribute /ff set
```

2.158 setAttributeList

```
ob attr setAttributeList new-obj
Example: [(x-1) (y-1)] [(gb) 1] setAttributeList /ff set
```

2.159 setMinus

```
a b setMinus c
```

2.160 shell

```
[gate-keeper f1 f2 ... fm] shell result
Sort the list. Gate-keeper should be the smallest element
```

2.161 sm1log

```
str sm1log outputs the str to the log file /tmp/sm1log.txt
```

2.162 swap01

```
[ .... ] swap01 [....]
Examples: [(x,y) ring_of_polynomials (x) elmination_order 0] swap01
          define_ring
```

2.163 swap0k

```
[ .... ] k swap0k [....]
Examples: [(x,y) ring_of_polynomials (x) elmination_order 0] 1 swap0k
          define_ring
swap01 == 1 swap0k
```

2.164 tag

```
obj tag integer
tag returns datatype.
cf. data_conversion
Example: 2 tag IntegerP eq ---> 1
```

2.165 tfbToTree

```
tfb-expression-in-string tfbToTree tree
tfbToTree translates expressions in tfb/2 into tree form.
Bug: the input is parsed by k0, so the symbol name given agrees with
     a k0 symbol, it returns a strange answer.
Example:  ( C+intpath.circle(0,1/2) ) tfbToTree ::
```

2.166 timer

```
 { codes } timer
It outputs the execution time to execute << codes >>.
If you type in ctrl-C while you are executing this macro,
you need to type in set_timer after you type in ctrl-C to reset
the timer.
```

2.167 toString

```
obj toString
Convert obj to a string.
Example: [ 1 (x+1). [ 2 (Hello)]] toString ==> $[ 1 , x+1 , [ 2 , Hello ]  ]$
```

2.168 toTokensBySpace

```
 string toTokensBySpace token_array
```

2.169 toVectors

```
obj toVectors vec
Convert the internal expression of vector into the array <<vec>>.
obj can be  [n [g1 ... gm]] where n is the length of the vector.
cf. [(toe_) array_of_poly] gbext
Example 1: [(x) ring_of_polynomials 0] define_ring
           (e_ + 2).  toVectors ::
```

```
        --->  [2  , 1]
Example 2: [3 (e_ +2).] toVectors ::
        ---> [2 , 1 , 0 ]
Example 3: [(e_+2). (e_^2+1).] toVectors ::
        ---> [[2 , 1] [1 , 0 , 1]]
Example 4: [2 [(e x + 1). (x+1).]] toVectors
           ===> [ [1 , x] [x+1 , 0] ]
```

2.170 toVectors2

```
Remained for the compatibility. cf. toVectors
```

2.171 to_int

```
obj to_int obj2
All integers in obj are changed to universalNumber.
Example: /ff [1 2 [(hello) (0).]] def  ff { tag } map ::
         ff to_int { tag } map ::
```

2.172 to_int32

```
obj to_int32 obj2
All universalNumber in obj are changed to integer (int32).
Example: /ff [1 (2).. [(hello) (0).]] def  ff { tag } map ::
         ff to_int32 { tag } map ::
cf. to_int, to_univNum
```

2.173 to_univNum

```
obj to_univNum obj2
Example. [ 2 (3).. ] to_univNum
cf. to_int32. (to_int)
```

2.174 tolower

```
string tolower string2
Capital letters in string are converted to lower case letters.
Example:  (Hello World) tolower :: (hello world)
```

2.175 transpose

```
 matrix transpose transposed_matrix
```

2.176 univ2poly

```
list univ2poly list2
Change universal numbers in list to an element of a ring of polynomials
defined by other elements in list. If there is no polynomial element,
the current ring is used.
```

2.177 usages

```
key usages usages-as-a-string
num usages list-of-key-words
[key1 key2 ... ] usages list-of-key-words  : it accepts regular expressions.
```

2.178 weight_vector

```
[x-list d-list params] [[(name) weight ...] [...] ...] weight_vector
[x-list d-list params order]
Example:
   [(x,y,z) ring_of_polynomials [[(x) 100 (y) 10]] weight_vector 0]
   define_ring
```

2.179 weightv

```
array weightv weight_vector_for_init
cf. init
Example: /w [(x) 10 (h) 2] weightv def
         ((x-h)^10).  w init ::
```

3 Macros in libraries

The macros described in this section can be used by loading library files by the command *cohom.sm*1 run `ox_asir` functions require open asir module.

```
var.sm1 : Version 3/7, 1997
ecart.minimalResol



lib/intw.sm1, Version 1999, 6/13. Package for integration with a generic weight.
integral-k1  wbf  intwbf tensor0 wTensor0 intwbfRoots wbfRoots wIntegration0
wRestriction0 ann-t-f bf-111 wdeRham0

Polymake is not installed in this system or @@@polymake.web is set.
Using doPolymake.OoHG.curl
```

3.1 Offverbose

```
Offverbose
Turn off all verbose flags of the packages. cf. Onverbose
```

3.2 Onverbose

```
Onverbose
Turn on all verbose flags of the packages. cf. Offverbose
```

3.3 ann-t-f

```
ann-t-f returns the annihilating ideal of delta(t-f(x))
Example: [(x^3-y^2) [(t) (x) (y)]] ann-t-f
```

3.4 annfs

```
 [ f v m r0] annfs g
It returns the annihilating ideal of f^m where r0 must be smaller
or equal to the minimal integral root of the b-function.
Or, it returns the annihilating ideal of f^r0, r0 and the b-function
where r0 is the minial integral root of b.
For the algorithm, see J. Pure and Applied Algebra 117&118(1997), 495--518.
Example 1: [(x^2+y^2+z^2+t^2) (x,y,z,t) -1 -2] annfs ::
           It returns the annihilating ideal of (x^2+y^2+z^2+t^2)^(-1).
Example 2: [(x^2+y^2+z^2+t^2) (x,y,z,t)] annfs ::
           It returns the annihilating ideal of f^r0 and [r0, b-function]
           where r0 is the minimal integral root of the b-function.
Example 3: [(x^2+y^2+z^2) (x,y,z) -1 -1] annfs ::
Example 4: [(x^3+y^3+z^3) (x,y,z)] annfs ::
Example 5: [((x1+x2+x3)(x1 x2 + x2 x3 + x1 x3) - t x1 x2 x3 )
            (t,x1,x2,x3) -1 -2] annfs ::
           Note that the example 4 uses huge memory space.

Note: This implementation is stable but obsolete.
As to faster implementation, we refer to ann0 and ann of Risa/Asir
Visit  http://www.math.kobe-u.ac.jp/Asir
```

3.5 appell1

```
param appell1 c
array param; array c;
appell1 returns an annihilating ideal for
the Lauricella function F_D(a,b_1, ..., b_n,c; x_1,...,x_n)
for the parameter << param >> = [a, c, b_1, ..., b_n].
In case of n=2, the function is called the Appell function F_1.
c = [ generators,  variables ]
Note that for a special set of parameters, the returned differential equation
is not holonomic, e.g., [[1 2 3 4]] appell1 rank ::
This happens because we do not included the Euler-Darboux operators
in the return value of appell1. It will be included in a future.
```

```
Example: [ [1 -4 -2 5 6] ] appell1 rank ::
For details, see P.Appell et Kampe de Feriet, Fonction hypergeometrique
et hyperspheriques -- polynomes d'Hermite, Gauthier-Villars, 1926.
```

3.6 appell4

```
param appell4 c
array param; array c;
appell4 returns an annihilating ideal for
the Lauricella function F_C(a,b, c_1, ..., c_n; x_1,...,x_n)
for the parameter << param >> = [a, b, c_1, ..., c_n].
In case of n=2, the function is called the Appell function F_4.
c = [ generators,  variables ]
Note that for a special set of parameters, the returned differential equation
is not holonomic, e.g., [[1 2 3 4]] appell4 rank ::
Example: [ [1 -4 -2 5 6] ] appell4 rank ::
```

3.7 asir

```
pid [asir-command, asir-arg1, asir-arg2, ...] asir result  (ox_asir function)
Call open asir server. You need to install ox_asir on your system
to use this function. cf. primadec, fctr, asirconnect2, asirconnectr.
If you interrupted the computation by typing ctrl-C, type in
   oxasir.ccc oxreset  ;
to interrupt the ox_asir server.
NOTE: all asir-args must belong to the same ring. cf.oxasir.changeRing.
Example: oxasir.ccc [(fctr) (x^10-1).] asir

This function requires plugins cmo, socket and ox_asir server. cf. oxasir
See, http://www.math.kobe-u.ac.jp/Asir on asir
```

3.8 asirconnectr

```
asirconnectr server  (ox_asir function)
array server;
Example: asirconnectr /oxasir.ccc set
```

3.9 bf-111

```
 [ideal vlist rest-vlist bf-111] bf-111
Compute the b-function for the weight vector 11111 for the variables
res-vlist.  cf. wbf
Example: [ [((x Dx -1 ) x Dx (x Dx + 2)) (y Dy)] (x,y) (x)] bf-111
```

3.10 bfunction

```
 a bfunction b
array a; poly b;
a :  [f] ;  string f ;
```

```
a :  [f] ;  polynomial f ;
a :  [f v] ; string f,v;
a :  [f v] ; polynomial f, string v;
b is the b-function (=Bernstein-Sato polynomial) of a polynomial f
in variables v.
If v is not specified, the variables are assumed to be (x,y,z).
b will be a polynomial in s.  This variable can be changed by typing in
  (variable) /bfunction.s set
For the algorithm, see Duke Math. J. 87 (1997),115-132,
   J. Pure and Applied Algebra 117&118(1997), 495--518.
Example  [(x^3-y^2) (x,y)] bfunction ::

See also bfct which implements a new algorithm to compute b-function and is faster. Aug 2002.
```

3.11 cgiPolymake

```
Make sm1 to a polymake server based on CGI/OoHG
 sm1 -q -s "[(parse) (cgi.sm1) pushfile] extension cgiPolymake quit "
```

3.12 ch

```
ch is the abbreviation of characteristic.
 a ch b
 array a;  number b
b is the generator of the characteristic variety of a.
For the algorithm, see, Japan J. of Industrial and Applied Math., 1994, 485--497.
Example 1 :
 [ [( (x Dx)^2 + ( y Dy)^2) ( x Dx y Dy -1)] (x,y)] ch ::
Example 2 :
[ [( (x^3-y^2) Dx + 3 x^2) ( (x^3-y^2) Dy - 2 y)] (x,y)] ch ::
```

3.13 characteristic

```
 a characteristic b
 array a;  number b
b is the generator of the characteristic variety of a.
For the algorithm, see Japan J. of Industrial and Applied Math., 1994, 485--497.
Example 1 :
 [ [( (x Dx)^2 + ( y Dy)^2) ( x Dx y Dy -1)] (x,y)] characteristic ::
Example 2 :
[ [( (x^3-y^2) Dx + 3 x^2) ( (x^3-y^2) Dy - 2 y)] (x,y)] characteristic ::
```

3.14 db.clear

```
db.clear cleans db.VariableStack
cf.  db.restore, db.where, db.clear.ds, db.clear.es, debugMode
```

3.15 db.clear.ds

```
db.clear.ds cleans db.DebugStack
cf.  db.where.ds, db.clear, debugMode
```

3.16 db.clear.es

```
db.clear.es cleans db.ErrorStack
cf.  db.clear, db.where.es
```

3.17 db.clear.es

```
db.clear.es cleans db.ErrorStack
cf.  db.clear, db.where.es
```

3.18 db.restore

```
db.restore recovers bindings of variables by reading db.VariableStack
cf. localVariables, restoreVariables,
    db.clear, db.where , debugMode
```

3.19 db.where

```
db.where shows the db.VariableStack
cf. localVariables, restoreVariables,
    db.clear, db.restore, db.where.ds, db.where.es, debugMode
```

3.20 db.where.es

```
db.where.es shows the db.ErrorStack
Error and warning messages are put in db.ErrorStack when the global
variables ErrorMessageMode or WarningMessageMode are set to 1 or 2.
cf. db.where, system_variable
```

3.21 deRham

```
[f v] deRham c
string f; string v;  f is a polynomial given by a string.
This function can be used by loading the experimental package cohom.sm1.
The dimensions of the deRham cohomology groups H^i(C^n - V(f),C) i=0, i=1, ..
.., n are returned in c.
For example, if c=[1 4 6 4], then it means that dim H^0(C^3-V(f),C) = 1,
dim H^1(C^3-V(f),C) = 4, and so on.
For the algorithm, see "An algorithm for de Rham cohomology groups of the
complement of an affine variety via D-module computation",
Journal of pure and applied algebra, 139 (1999), 201--233. math.AG/9801114

Example 0:  [(x (x-1) (x-2)) (x)] deRham
```

```
Example 1: [(x y (x+y-1)(x-2)) (x,y)] deRham
Example 2: [(x^3-y^2) (x,y)] deRham
Example 3: [(x^3-y^2 z^2) (x,y,z)] deRham
Example 4: [(x y z (x+y+z-1)) (x,y,z)] deRham
```

3.22 debugMode

```
debugMode overrides on the functions pushVariables and popVariables
and enables to use db.where.  Never execute debugMode inside a block of
pushVariables and popVariables
```

3.23 doPolyamke.OoHG

```
The keyword <<doPolyamke.OoHG>> cannot be found.
Type in ? in order to see system dictionary.
```

3.24 ecart.gb

```
a ecart.gb b
array a; array b;
b : [g ii];  array g; array in; g is a standard (Grobner) basis of f
             in the ring of differential operators.
The computation is done by using Ecart division algorithm and
the double homogenization.
cf. M.Granger and T.Oaku: Minimal filtered free resolutions ... 2003
           ii is the initial ideal in case of w is given or <<a>> belongs
           to a ring. In the other cases, it returns the initial monominal.
a : [f ];    array f;  f is a set of generators of an ideal in a ring.
a : [f v];   array f; string v;  v is the variables.
a : [f v w]; array f; string v; array of array w; w is the weight matirx.
a : [f v w [(degreeShift) ds]]; array f; string v; array of array w; w is the weight matirx.
                array ds; ds is the degree shift for the ring.
a : [f v w [(degreeShift) ds (startingShift) hdShift]]; array f; string v; array of array w; w is the weight
        array ds; ds is the degree shift for the ring.
        array hsShift is the degree shift for the homogenization. cf.homogenize
a : [f v w [(degreeShift) ds (noAutoHomogenize) 1]]; array f; string v; array of array w; w is the weight mat
       No automatic homogenization.
  [(degreeShift) ds (noAutoHomogenize) 1 (sugar) 1] -->use the sugar strate

cf. ecarth.gb (homogenized),  ecartd.gb (dehomogenize), ecartd.reduction
    ecartd.gb.oxRingStructure

Example 1: [ [( (x Dx)^2 + (y Dy)^2 -1) ( x y Dx Dy -1)] (x,y)
             [ [ (Dx) 1 ] [(x) -1 (y) -1 (Dx) 1 (Dy) 1]] ] ecart.gb pmat ;
Example 2:
 [ [(2 x Dx + 3 y Dy+6) (2 y Dx + 3 x^2 Dy)] (x,y)
   [[(x) -1 (Dx) 1 (y) -1 (Dy) 1]]] ecart.gb  /ff set ff pmat ;
To set the current ring to the ring in which ff belongs
      ff getRing ring_def

Example 3: [ [( (x Dx)^2 + (y Dy)^2 -1) (  x y Dx Dy -1)] (x,y)
             [ [ (Dx) 1 (Dy) 1] ] ] ecart.gb pmat ;
```

```
   This example will cause an error on order.

Example 4: [[ [(x^2) (y+x)] [(x+y) (y^3)] [(2 x^2+x y) (y+x+x y^3)]] (x,y)
             [ [ (x) -1 (y) -1] [(x) -1 (y) -1 (Dx) 1 (Dy) 1]] ] ecart.gb pmat ;
   This example will cause an error on order.

Example 5: [[ [(x^2) (y+x)] [(x+y) (y^3)] [(2 x^2+x y) (y+x+x y^3)]] (x,y)
             [ [(Dx) 1 (Dy) 1] [(x) -1 (y) -1 (Dx) 1 (Dy) 1] ]
             [(degreeShift) [[0 1] [-3 1]]] ] ecart.gb pmat ;

Example 6:  [ [(1-z) (-x+1-y-z)] (x,y,z)
              [[(y) -1 (z) -1 (Dy) 1 (Dz) 1] [(x) 1 (Dx) 1]]
              [(partialEcartGlobalVarX) [(x)]] ] /std set
             std ecart.gb pmat ;
             std ecart.gb getRing ::

cf. gb, groebner, ecarth.gb, ecartd.gb, ecart.syz, ecart.begin, ecart.end, ecart.homogenize01,
    ecart.dehomogenize, ecart.dehomogenizeH
 [(weightedHomogenization) 1 (degreeShift) [[1 2 1]]] : options for
                                                         define_ring
/ecart.autoHomogenize 0 def
               not to dehomogenize and homogenize
```

3.25 ecart.minimalBase

```
[ff v ecart.weight_vector [(degreeShift) uv_shift_m (startingShift) [D_shift_n uv_shift_m]]]  ecart.minimalBa
  [mbase gr_of_mbase
     [syz v ecart.weight_vector [(degreeShift) new_uv_shift_m (startingShift) [new_D_shift_n new_uv_shift_m]]
     gr_of_syz ]
mbase is the minimal generators of ff in D^h in the sense of filtered minimal
generators.
Example: [ [(t-x^3+y^2) (Dx+ 3 x^2 Dt) (Dy - 2 y Dt)] (t,x,y)
           [ [(t) -1 (Dt) 1] [(t) -1 (x) -1 (y) -1 (Dt) 1 (Dx) 1 (Dy) 1]]
           [(degreeShift) [ [0] ]
            (startingShift) [ [0] [0] ] ] ] ecart.gen_input /gg0 set
         gg0 ecart.minimalBase /ss0 set
         ss0 2 get ecart.minimalBase /ss1 set
         ss1 2 get ecart.minimalBase /ss2 set
     (---------  minimal filtered resolution -------) message
     ss0 0 get pmat ss1 0 get pmat ss2 0 get pmat
     (---------  degree shift (n,m) n:D-shift m:uv-shift  -------) message
     gg0      3 get 3 get message
     ss0 2 get 3 get 3 get message
     ss1 2 get 3 get 3 get message
     ss2 2 get 3 get 3 get message ;
```

3.26 ecart.minimalResol

```
[ff v ecart.weight_vector [(degreeShift) uv_shift_m (startingShift) [D_shift_n uv_shift_m]]]  ecart.minimalRe
  [resol degree_shifts gr_of_resol_by_uv_shift_m]
Example1: [ [(t-x^3+y^2) (Dx+ 3 x^2 Dt) (Dy - 2 y Dt)] (t,x,y)
           [ [(t) -1 (Dt) 1] [(t) -1 (x) -1 (y) -1 (Dt) 1 (Dx) 1 (Dy) 1]]
           [(degreeShift) [ [0] ]
            (startingShift) [ [0] [0] ] ] ] ecart.minimalResol /gg set gg pmat
```

3.27 ecart.syz

```
a ecart.syz b
array a; array b;
b : [syzygy gb tmat input];  gb = tmat * input
Example 1: [ [( (x Dx)^2 + (y Dy)^2 -1) (  x y Dx Dy -1)] (x,y)
             [ [ (Dx) 1 (Dy) 1] [(x) -1 (y) -1 (Dx) 1 (Dy) 1]] ] ecart.syz /ff set
 ff 0 get ff 3 get mul pmat
 ff 2 get  ff 3 get mul [ff 1 get ] transpose sub pmat ;

To set the current ring to the ring in which ff belongs
      ff getRing ring_def
Example 2: [[ [(x^2) (y+x)] [(x+y) (y^3)] [(2 x^2+x y) (y+x+x y^3)]] (x,y)
             [ [(Dx) 1 (Dy) 1] [ (x) -1 (y) -1] ]  [[0 1] [-3 1] ] ] ecart.syz pmat ;

cf. ecart.gb
    /ecart.autoHomogenize 0 def
```

3.28 ecartd.reduction

```
f basis ecartd.reduction r
f is reduced by basis by the tangent cone algorithm.
The first element of basis <g_1,...,g_m> must be a standard basis.
r is the return value format of reduction.
r=[h,c0,syz,input], h = c0 f + \sum syz_i g_i
basis is given in the argument format of ecartd.gb.
h[0,1](D)-homogenization is used.
cf. reduction, ecartd.gb, ecartd.reduction.test
Example:
 [[( 2*(1-x-y) Dx + h ) ( 2*(1-x-y) Dy + h )]
   (x,y) [[(Dx) 1 (Dy) 1] [(x) -1 (y) -1 (Dx) 1 (Dy) 1]]] /ggg set
 (Dx+Dy) ggg ecartd.reduction ::
```

3.29 extension-oxLog

```
Take the log of communication in files.
[(oxLog) client logfile_for_incomming_data logfile_for_outgoing_data] extension
Example:
  [(parse) (ox.sm1) pushfile] extension
  sm1connectr
  (i.t) (w) file /ii set
  (o.t) (w) file /oo set
  [(oxLog) oxsm1.ccc ii oo] extension
  [(oxWatch) oxsm1.ccc ] extension
  oxsm1.ccc 1 oxpushcmo ;
  oxsm1.ccc oxpopcmo ;
  [(oxLogStop) oxsm1.ccc] extension
```

3.30 fctr

```
You need to install ox_asir server to use this function. (ox_asir function)
f fctr g
poly f; array g;
[f v] fctr g ;  string f, string or array of string v
This function factors the polynomial f over Q.

Example 1:  [(x^10-y^10) (x,y)] fctr ::
Example 2:  (x^10-1). fctr ::

If you interrupted the computation by typing ctrl-C, type in
   oxasir.ccc oxreset  ;
to interrupt the ox_asir server.

This function requires plugins cmo, socket and ox_asir server. cf.oxasir
```

3.31 gb

```
a gb b
array a; array b;
b : [g ii];  array g; array in; g is a Grobner basis of f
             in the ring of differential operators.
            ii is the initial ideal in case of w is given or <<a>> belongs
            to a ring. In the other cases, it returns the initial monominal.
a : [f ];    array f;  f is a set of generators of an ideal in a ring.
a : [f v];   array f; string v;  v is the variables.
a : [f v w]; array f; string v; array of array w; w is the weight matirx.
a : [f v w ds]; array f; string v; array of array w; w is the weight matirx.
                array ds; ds is the degree shift

gb.authoHomogenize 1 [default]
gb.oxRingStructure

Example 1: [ [( (x Dx)^2 + (y Dy)^2 -1) ( x y Dx Dy -1)] (x,y)
             [ [ (Dx) 1 ] ] ] gb pmat ;
Example 2:
To put h=1, type in, e.g.,
 [ [(2 x Dx + 3 y Dy+6) (2 y Dx + 3 x^2 Dy)] (x,y)
   [[(x) -1 (Dx) 1 (y) -1 (Dy) 1]]] gb /gg set gg dehomogenize pmat ;

Example 3: [ [( (x Dx)^2 + (y Dy)^2 -1) (  x y Dx Dy -1)] (x,y)
             [ [ (Dx) 1 (Dy) 1] ] ] gb pmat ;

Example 4: [[ [(x^2) (y+x)] [(x+y) (y^3)] [(2 x^2+x y) (y+x+x y^3)]] (x,y)
             [ [ (x) -1 (y) -1] ] ] gb pmat ;

Example 5: [[ [(x^2) (y+x)] [(x+y) (y^3)] [(2 x^2+x y) (y+x+x y^3)]] (x,y)
             [ [ (x) -1 (y) -1] ]  [[0 1] [-3 1] ] ] gb pmat ;

Example 6: [ [( (x Dx)^2 + (y Dy)^2 - x y Dx Dy + 1) ( x y Dx Dy -1)] (x,y)
             [ [ (Dx) 1 ] ] ] [(reduceOnly) 1] setAttributeList gb pmat ;

Example 7: [ [( (x Dx)^2 + (y Dy)^2 + 1) ( x y Dx Dy -1)] (x,y)
     [ [ (Dx) 1 ] ] ] [(gbCheck) 1] setAttributeList gb getAttributeList ::
```

```
Example 8: /gb.options [(StopDegree) 11] def Onverbose
 [ [(x^10+y^10-1) (x^5*y^5 -1)] (x,y)
     [ [ (x) 1 ] ]]  gb pmat ;

cf. gb, groebner, groebner_sugar, syz.
```

3.32 genericAnn

```
f [s v1 v2 ... vn] genericAnn [L1 ... Lm]
L1, ..., Lm are annihilating ideal for f^s.
f is a polynomial of v1, ..., vn
<string> | <poly>  f, s, v1, ..., vn ; <poly>  L1, ..., Lm
Example: (x^3+y^3+z^3) [(s) (x) (y) (z)] genericAnn
```

3.33 genericAnnWithL

```
[f v] genericAnnWithL [b [L I]]
String f,v; poly b,L; array of poly I;
f is a polynomial given by a string. v is the variables.
 v must not contain names  s, e.
b is the b-function (Bernstein-Sato polynomial) for f and
 L is the operator satisfying L f^{s+1} = b(s) f^s
 I is the annihilating ideal of f^s.
cf. bfunction, annfs, genericAnn.
Example 1:  [(x^2+y^2) (x,y)] genericAnnWithL ::
Example 2:  [(x^2+y^2+z^2) (x,y,z)] genericAnnWithL ::
Example 3:  [(x^3-y^2 z^2) (x,y,z)] genericAnnWithL ::
```

3.34 gfan

```
gfan.sm1 is a package to compute global and local Grobner fans.
See  R.Bahloul and N.Takayama, arxiv, math.AG/0412044 and references as to algorithms.
At the beginning of the source code gfan.sm1, there are sample inputs cone.sample and cone.sample2.

gfan.sm1 works only with polymake 2.0. We provide a web service of computing
with polymake 2.0.  /@@@polymake.web 1 def is set by default in gfan.sm1.
See changelog-ja.tex as to details on the difference between 2.0 and later versions.

*cone.sample ; is an example. See the source code. The state polytope is the hexagon.

*cone.Wt cone.Lpt {vertices in the output} are weights on the rays of the Grobner cone.
*cone.L gives a basis of the linearity space.
*cone.Lp gives a basis of the pointed cone. cone.Lpt is the transpose of cone.Lp.
*When v is a row vector in an ouput cone, (v cone.Lp cone.W) gives
  the corresponding weight vector in the full variable space in D
*cone.incidence is a list of [[cone num1,facet num1], [cone num2,facet num2]]
  which means that cone num1 and cone num2 are adjacent and shares
  the facet num1 and the facet num2
*/cone.withGblist 1 def saves the Grobner basis standing for each cone.

*Cone descriptions: cone.fan
**A facet is given by its normal vector n of a cone. It gives facet num of the cone.
**A cone is defined by facet normal vectors n1, n2, ... as n1.x>=0 and n2.x >=0 and ...
```

```
**facetsv is a list of facets expressed by generators.
**nextcid is a list of the adjacent cone numbers.
**nextfid is a list of the shared facet numbers.
**vertices is the generators of a cone.
**inequalities are not necessarily unique.
```

3.35 gkz

```
[ A b] gkz [eq v]
[ A  ] gkz [eq v]
[    ] gkz [eq v]
array of array of integer A; array of integer b;
eq is the GKZ system defined by the matrix A and the parameter b.
v is the list of variables.
Default values of A and b are in gkz.A and gkz.b
For details, see Functional analysis and its applications, 23, 1989, 94--106.
    Grobner deformations of hypergeometric differential equations, Springer, 1999
Example 1: [ [[1 1 1 1] [0 1 3 4]] [1 2]] gkz rrank ::
Example 2: [ [[1 1 1 1] [0 1 3 4]] [0 0]] gkz rrank ::
```

3.36 integral-k1

```
[[f1 ... fm] [v1 ... vn] [v1 w1 ... vp wp] k1] integral0
                                              [[g1 ... gq],[e1,...,er]]
poly|string f1 ...fm; string v1 ... vn;
string v1 ... vp; integer w1 ... wp;
integer k1;
poly g1 ... gq; poly e1, ..., er;
f1 ... fm are annihilors, v1 ... vn are variables,
w1 is the weight of the variable v1, ...
k1 is the maximal degree of the filtration: maximal integral root
of b-function. cf. intwbf
g1, ..., gq are integral. e1, ..., er are basis of the free module to which
the g1, ..., gq belong.
THE ORDERS OF INTEGRAL VARIABLES MUST BE SAME BOTH IN THE SECOND AND
THE THIRD ARGUMENTS. INTEGRAL VARIABLES MUST APPEAR FIRST.
Example 1: [[(x-y) (Dx+Dy)] [(y) (x)] [(y) -1 (Dy) 1] 1] integral-k1
Example 2: [[(x (x-1)) (x)] annfs 0 get [(x)] [(x) -1 (Dx) 1] 1] integral-k1
Example 3: [[ (Dt- (2 t x1 + x2)) (Dx1 - t^2) (Dx2 - t) ]
             [(t) (x1) (x2)] [(t) -1 (Dt) 1] 0] integral-k1
           The resulting ideal annihilates f(x1,x2)=int(x1*t^2+x2*t,dt)
```

3.37 integration

```
 [[f1 f2 ...] [t1 t2 ...] [vars params] [k0 k1 limitdeg ]] integration
  [ 0-th cohomology group,  (-1)-th cohomology group, .... ]

 [[f1 f2 ...] [t1 t2 ...] [vars params] limitdeg] integration

This function can be used by loading the experimental package cohom.sm1.
Integration of the D-ideal [f1 f2 ...] to t1=0, t2=0, ... is computed.
vars is a list of the variables and params is a list of parameters.
k0 is the minimum integral root of the b-function and k1 is the maximum
```

```
integral root of the b-function. If these values are not given and
they are small, then they are automatically computed. The program returns
 0-th, ..., -limitdeg-th cohomology groups.
[vars params] and [k0 k1 deg] are optional arguments.
If vars and params are not given, the values of the global variables
BFvarlist and BFparlist will be used.
The operator restriciton will be used after the laplace transformation.

For the algorithm, see math.AG/9805006, http://xxx.langl.gov

Example 1:
[[(x (x-1)) (x) ] annfs 0 get       [(x)] [[(x)] [ ]]] integration ::
Example 2:
[ [(Dt - (3 t^2-x)) (Dx + t)] [(t)]      [[(t) (x)] [ ]] 0] integration ::
Example 3:
[ [[(Dt - (3 t^2-x)) (0)] [ (Dx + t) (0)]] [(t)]      [[(t) (x)] [ ]] 0] integration ::
In case of vector input, INTEGRAL VARIABLES MUST APPEAR FIRST
in the list of variable. We are using wbfRoots to get the roots of
b-functions, so we can use only generic weight vector for now.
```

3.38 intersection

```
Ideal intersections in the ring of differential operators.
[ I1 I2 V-list ] intersection  : I1 and I2 are ideals, and V-list
is a list of variables.  It returns the ideal intersection of I1 and I2.
Intersection is computed in the ring of differential operators.
Example 1: [[[(x1) (x2)] [(x2) (x4)] (x1,x2,x3,x4)] intersection
             [(x2) (x4^2)] (x1,x2,x3,x4)] intersection ::
Example 2: [[[(x1) (x2)] [(x2) (x4)] (x1,x2,x3,x4)] intersection
             [(x2) (x4^2)] (x1,x2,x3,x4)] intersection /ff set ff message
           [ ff [(x2^2) (x3) (x4)] (x1,x2,x3,x4)] intersection ::
Example 3: [[[(x1) (x2)] [(x2) (x4^2)] (x1,x2,x3,x4)] intersection
             [(x2^2) (x3) (x4)] (x1,x2,x3,x4)] intersection ::
```

3.39 intwbf

```
[[f1 ... fm] [v1 ... vn] [v1 w1 ... vp wp]] intwbf [g1 ... gq]
<poly>|<string> f1 ...fm; <string> v1 ... vn;
<string> v1 ... vp; <integer> w1 ... wp;
<poly> g1 ... gq;
f1 ... fm are generators, v1 ... vn are variables,
w1 is the weight of the variable v1, ...
THE ORDERS OF INTEGRAL VARIABLES MUST BE SAME BOTH IN THE SECOND AND
THE THIRD ARGUMENTS. INTEGRAL VARIABLES MUST APPEAR FIRST.
If the weight is not generic, then the function exits with error.
Example 1: [[(x-y) (Dx+Dy)] [(y) (x)] [(y) -1 (Dy) 1]] intwbf
            integrate only for y.
Example 2: [[(-3 x^2 Dy-2 y Dx) (2 x Dx+3 y Dy+6)] [(x) (y)]
            [(x) -1 (Dx) 1 (y) -2 (Dy) 2]] intwbf
Example 3: [[[(0) (x^2 Dx+x)] [(Dx^2+x Dx^3) (0)]] [(x)]
            [(x) -1 (Dx) 1]] intwbf
```

3.40 intwbfRoots

```
This function needs oxasir  --- rationalRoots2
This function is defined in intw.sm1 and requires oxasir.sm1 and ox_asir server.
Example 1:  [[(-3 x^2 Dy-2 y Dx) (2 x Dx+3 y Dy+6)] [(x) (y)]
             [(x) -1 (Dx) 1 (y) -2 (Dy) 2]] intwbfRoots
Example 2:   [[[(0) (x^2 Dx+x)] [(Dx^2+x Dx^3) (0)]] [(x)]
               [(x) -1 (Dx) 1]] intwbfRoots
```

3.41 loadAsirFile

```
[client fname] loadAsirFile   (ox_asir function)
Load a file into the client
```

3.42 localVariables

```
This function is as same as pushVariables, but it pushes the variable to
db.VariableStack
cf. db.where, pushVariables, restoreVariables, debugMode
```

3.43 mgkz

```
[A w b] gkz [eq v]
[    ] gkz [eq v]
array of array of integer A; array of integer w, b;
eq is the modified GKZ system defined by the matrix A, weight w,
and the parameter b.
v is the list of variables. The last variable is the deformation variable.
Default values of A and b are in gkz.A and gkz.b
For details, see the paper Modified A-hypergeometric system, N.Takayama
http://arxiv.org/abs/0707.0043
Example : [ [[1 2 3]] [1 2 1] [0]] mgkz rank ::
Example : [ [[1 2 3]] [0]] gkz rank ::
Example : [ [[1 1 1] [1 2 3]] [1 2 1] [1 0]] mgkz message
```

3.44 ox

```
client aa oxpushcmo (oxsendcmo), client oxpopcmo dd, client popstring dd, client ss oxrpc
Example: oxsm1.ccc [1 2 3] oxpushcmo oxsm1.ccc oxpopcmo /ff set  ff ::

client ss oxexecutestring(oxsubmit) <<executeString>>, client ss oxexec <<executeFunction>>
client ss oxexecWithOpt
Example: oxsm1.ccc (0 1 10 { pop $Hello$ message } for) oxexecutestring
Example: oxsm1.ccc (2).. oxpushcmo oxsm1.ccc (10).. oxpushcmo
         oxsm1.ccc (power) oxexec  oxsm1.ccc oxpopcmo ::

client str oxevalname, client str oxsetname, client num oxpops, client oxget

client oxmathcap, client oxsetmathcap, oxgenportfile, oxremoveportfile
client oxpushcmotag
```

```
client oxgetsp --- get stack pointer,  client oxgeterrors --- get all errors
client oxclearstack --- clear the stack of the ox server.
cleint oxisData, client oxreset, client oxshutdown
oxhelp for this message
[(oxWatch) client] extension to start a log.
        ex 1.  (ox.sm1) run sm1connectr [(oxWatch) oxsm1.ccc] extension
               oxsm1.ccc ( [(cmoLispLike) 0] extension ) oxsubmit
               oxsm1.ccc ( [(cmoLispLike) 1] extension ) oxsubmit
[(oxSerial)] extension serial-number-of-out-going-ox-packet.
oxpopcmo1, oxpopcmo2, sm1connectr ox_launch, ox_launch_nox
oxNoX : set an environment to invoke oxlog without xterm and to call oxlog with >& /dev/null
        ex 1.  (ox.sm1) run oxNoX sm1connectr
        ex 2.  (ox.sm1) run oxNoX (x^2-1). fctr pmat ;

cf. extension-oxLog
oxMonitor : ox_sm1 server outputs packet dumps.
        ex 1. (ox.sm1) run oxMonitor sm1connectr
```

3.45 ox_launch

```
 [remote-machine remote-ox-server-name remote-login-name]
  ox_launch  client
or
 [(localhost) ox-server-name] ox_launch client
This command launches ox server via ssh.
My hostname is set by the function gethostname.
Example 1:
 [(orange2-clone)
  (bin/ox_sm1) (taka)
 ] ox_launch /@@@.oxsm1 set
```

3.46 ox_launch_nox

```
 [remote-machine remote-ox-server-name remote-login-name]
  ox_launch_nox  client
Example 1:
 [(tau.math.kobe-u.ac.jp)
  (bin/ox_math) (taka)
 ] ox_launch_nox /@@@.oxmath set
```

3.47 oxconnect

```
The keyword <<oxconnect>> cannot be found.
Type in ? in order to see system dictionary.
```

3.48 pgb

```
a pgb b
array a; array b;
b : [g ii];  array g; array in; g is a Grobner basis of f
```

```
             in the ring of polynomials.
             ii is the initial ideal in case of w is given or <<a>>belongs
             to a ring. In the other cases, it returns the initial monominal.
a : [f ];    array f;  f is a set of generators of an ideal in a ring.
a : [f v];   array f; string v;  v is the variables.
a : [f v w]; array f; string v; array of array w; w is the weight matirx.
Example 1: [(x,y) ring_of_polynomials 0] define_ring
           [ [(x^2+y^2-4). (x y -1).] ] pgb ::
Example 2: [ [(x^2+y^2) (x y)]   (x,y)  [ [(x) -1 (y) -1] ] ] pgb ::
Example 3: [ [(x^2+y^2 + x y ) (x y)]   (x,y)  [ [(x) -1 (y) -1] ] ]
           [(reduceOnly) 1] setAttributeList pgb ::
cf. gb, groebner, groebner_sugar, syz.
```

3.49 primadec

```
You need to install ox_asir server to use this function. (ox_asir function)
[ ii ] primadec [[q1 p1] [q2 p2] ... ]
 array of poly ii; array of poly q1, p1, q2, p2 ...;
 q1, q2, ... are primary components of the primary ideal decomposition
 of the ideal generated by << ii >>.

[ ii v ] primadec [[q1 p1] [q2 p2] ... ]
 array of poly or string ii; array of string v; array of poly q1, p1, q2, p2 ...;
<< v >> is an array of independent variables.

[ ii v ] primadec [[q1 p1] [q2 p2] ... ]
 array of poly or string ii; array of string v; array of poly q1, p1, q2, p2 ...;
 v  is a string of variables separated by ,

Example:  [(x,y) ring_of_polynomials 0] define_ring
          [ [(x^2-1). (x y).] ] primadec pmat ;

Example:  [ [(x^2-1) (x y)] [(x) (y)]] primadec pmat ;

If you interrupted the computation by typing ctrl-C, type in
   oxasir.ccc oxreset  ;
to interrupt the ox_asir server.

This function requires plugins cmo, socket and ox_asir server. cf.oxasir
```

3.50 ptozp_subst

```
[f  s  [p q] v] ptozp_subst g   (ox_asir function)
It returns ptozp(subst(f,s,p/q))
Example 1:  [ (x Dx - s) (s) [2 3] (x,s)] ptozp_subst
   ===>     3 x Dx - 2
```

3.51 rank

```
 a rank b
 array a;  number b
Example 1 :
 [ [( (x Dx)^2 + ( y Dy)^2) ( x Dx y Dy -1)] (x,y)] rank ::
```

```
Example 2 :
[ [( (x^3-y^2) Dx + 3 x^2) ( (x^3-y^2) Dy - 2 y)] (x,y)] rank ::
```

3.52 reduceByAsir

```
 [[f g] v] reduceByAsir [ff gg]   (ox_asir function)
 [[f g]] reduceByAsir [ff gg]
Example 1: [[(2 x -2) (4 x - 8)] (x)] reduceByAsir
Note that there may be a gcd that is more than 1 among the coefficients.
```

3.53 res-div

```
 [M N] res-div K
 matrix M, N, K ; Each element of M and N must be an element of a ring.
 coker(K) is isomorphic to M/N.
Example: [(x,y) ring_of_differential_operators 0] define_ring
   [[[(x+x^2+y^2).] [(x y).]] [[(x+x^2+y^2).] [(x y).]]] res-div

res*div accepts string inputs, too. For example,
 [[[[(x+x^2+y^2)] [(x y)]] [[(x+x^2+y^2)] [(x y)]]]
   [(x) (y)]]  res*div ::
See also res-toString, res-setRing.
```

3.54 res-dual

```
[F V] res-dual G
G is the dual D-module of F. V is a list of variables.
Example 1:  [ [( x^3-y^2 )  ( 2 x Dx + 3 y Dy + 6 )  ( 2 y Dx + 3 x^2 Dy) ]
              [(x) (y)]] res-dual
Example 2:  [[1 3 4 5]] appell1 res-dual
Example 3:  [ [(-x1 Dx1 + x1 + 2) (x2 Dx2 - Dx2 -3)] [(x1) (x2)]] res-dual
Example 4:  [ [(x2 Dx2 - Dx2 + 4) (x1 Dx1 + x1 +3)] [(x1) (x2)]] res-dual
            3 and 4 are res-dual each other.
Example 5:  [ [[1 1 1][0 1 2]] [0 0]] gkz res-dual
Example 6:  [ [[1 1 1][0 1 2]] [-2 -1]] gkz res-dual

Example 7:  [ [(x Dx -1) (Dx^2)]     [(x)]] res-dual
Example 8:  [ [[(1) (0)] [(0) (Dx)]] [(x)]] res-dual
Example 9:  [ [((x Dx + x +1) (Dx-1))] [(x)]] res-dual
```

3.55 res-kernel-image

```
 [m n vlist] res-kernel-image c
When, D^p <-- m --- D^q <-- n -- D^r
D^q/c is isomorhic to ker(m)/im(n).
vlist is a list of variables.
```

3.56 res-solv

```
[M d] res-solv [c' r]
 M : matrix,  d, c' : vectors, r : scalar(integer)
 c:=c'/r is a solutions of Sum[c_i M_i] = d where c_i is the i-th element
 of the vector c and M_i is the i-th row vector of M.
If there is no solution, then res-solv returns null.
Note that M and d are not treated as an element of the homogenized Weyl
algebra. If M or d contains the homogenization variable h, it automatically
set to 1. If you need to use h, use the command res-solv-h
[M d rng] res-solv [c' r]
 rng is a ring object.
 res-solv extracts variables names from rng, but defines a new ring.
Example 1:  [(x,y) ring_of_differential_operators [[(x) -1 (Dx) 1]] weight_vector 0]
              define_ring
 [ [ [(x Dx + 2).] [ (Dx (x Dx + 3) - (x Dx + 2) (x Dx -4)).]]   [(1).]]
  res-solv ::
Example 2:
 [ [ (x Dx + 2).  (Dx (x Dx + 3) - (x Dx + 2) (x Dx -4)).]   (1).]
  res-solv ::
Example 3:
 [ [[(x Dx + 2). (0).]
    [(Dx+3).     (x^3).]
    [(3).        (x).]
    [(Dx (x Dx + 3) - (x Dx + 2) (x Dx -4)). (0).]]   [(1). (0).]]
  res-solv ::
Example 4:
 [[ (x*Dx+h^2). (Dx^2+x*h).] [(x^2+h^2). (h Dx + x^2).]] /ff set
 [[ (x^2 Dx + x h^2). (Dx^3).]] /gg set
 [ff gg ff mul 0 get ] res-solv-h ::

res*solv and res*solv*h accept string inputs, too. For example,
 [[ [ [(x Dx + 2)] [ (Dx (x Dx + 3) - (x Dx + 2) (x Dx -4))]]   [(1)]]
  (x)]  res*solv ::
```

3.57 resol0

```
 [ ii v] resol0 r
array of poly ii; string v;
<< vv >> is a string of variables separated by ,

 [ ii v] resol0 r
array of poly ii; array of strings v;
<< vv >> is an array of variable names.

 [ ii v w] resol0 r
array of poly ii; string v; array w;
<< w >> is a weight vector.

You can also give a parameter << d >> to specify the truncation depth
of the resolution: [ d ii v] resol0, [d ii v w] resol0

resol0 constructs a resolution which is adapted (strict)
to a filtration. So, it is not minimal.
 r = [starting Groebner basis g, [ s1, s2 , s3, ...], order-def].
g is the reduced Groebner basis for f,
```

```
 s1 is the syzygy of g,
 s2 is the syzygy of s1,
 s3 is the syzygy of s2 and so on.
For details, see math.AG/9805006
cf. sResolution, tparse, s_ring_..., resol0.cp
Example:  [ [( x^3-y^2 )  ( 2 x Dx + 3 y Dy + 6 )  ( 2 y Dx + 3 x^2 Dy) ]
             (x,y) ] resol0 ::
```

3.58 resol1

```
 [ ii v] resol1 r
array of poly ii; string v;
<< vv >> is a string of variables separated by ,

 [ ii v] resol1 r
array of poly ii; array of strings v;
<< vv >> is an array of variable names.

 [ ii v w] resol1 r
array of poly ii; string v; array w;
<< w >> is a weight vector.

 ii may be array of array of poly.
You can also give a parameter << d >> to specify the truncation depth
of the resolution: [ d ii v] resol1, [d ii v w] resol1

resol1 constructs a resolution which is adapted (strict)
to a filtration. So, it is not minimal in general.
 r = [s0, s1, s2 , s3, ...].
 s0 is the groebner basis of ii,
 s1 is the syzygy of s0,
 s2 is the syzygy of s1,
 s3 is the syzygy of s2 and so on.
 s1 s0 mul ==> 0, s2 s1 mul ==>0, ...
For details, see math.AG/9805006
cf. sResolution, tparse, s_ring_..., resol0.cp
resol1.withZeroMap returns a resolution with zero maps of the both sides
   of the resolution.
cf. resol1.zeroMapL, resol1.zeroMapR, resol1.withZeroMap.aux
resol1.syzlist : global variable to keep the raw output of sResolution.

Example 1: [ [( x^3-y^2 )  ( 2 x Dx + 3 y Dy + 6 )  ( 2 y Dx + 3 x^2 Dy) ]
             (x,y) ] resol1 pmat ;
Example 2: [ [( x^3-y^2 )  ( 2 x Dx + 3 y Dy + 6 )  ( 2 y Dx + 3 x^2 Dy) ]
             (x,y) [[(x) -1 (Dx) 1 (y) -1 (Dy) 1]]] resol1 pmat ;
Example 3: [ [[(2 x Dx + 3 y Dy +6) (0)]
              [(3 x^2 Dy + 2 y Dx) (0)]
              [(0) (x^2+y^2)]
              [(0) (x y )] ]
             (x,y) [[(x) -1 (Dx) 1 (y) -1 (Dy) 1]]] resol1 pmat ;
Example 4:  /resol0.verbose 1 def
          [ [[(x^2+y^2+ x y) (x+y)] [(x y ) ( x^2 + x y^3)] ] (x,y)
            [[(x) -1 (Dx) 1 (y) -1 (Dy) 1]]] resol1 pmat ;
```

3.59 restall_s

```
f v s_0 s_1 level restall_s c
array f; array v; integer s_0, s_1, level; array c
f is a set of generators. v is a set of variables.
s_0 is the minimal integral root of the b-function.
s_1 is the maximal integral root of the b-function.
level is the truncation degree of the resolution.
c is the cohomolgy.
This command is vector clean for Schreyer 1 and 2.

Global variables: array BFvarlist : list of variables.
                  array BFparlist : list of parameters.
                  int BFmessage : verbose or not.
                  int Schreyer : Schreyer 1 with tower-sugar.sm1 -- V-homog.
                                 Schreyer 2 with tower.sm1 --- H-homog.
                                 Schreyer 0 is a step by step resolution.
result global var:array BFresolution : resolution matrices.

cf. /tower.verbose 1 def /tower-sugar.verbose 1 def
    /debug.sResolution 1 def
       to see steps of resoluitons.
  /Schreyer 2 def  (tower.sm1) run   to try Schreyer 2. Schreyer 2 is default.
See bfm --- b-function, restriction.
restall1_s is as same as restall_s, except it does not truncate from below.
Example 1:  /BFvarlist [(x1) (x2)] def /BFparlist [ ] def
            [(x1) (Dx2-1)] [(x1)] -1 -1 1 restall_s
Example 1a: /BFvarlist [(x1) (x2)] def /BFparlist [ ] def
            [(x1) (Dx2-1)] [(x1)] bfm
Example 2:  /BFvarlist [(x) (y)] def /BFparlist [ ] def
 [[(x Dx -1) (0)] [(y Dy -2) (0)]  [(1) (1)] ] /ff set
 ff [(x) (y)] 0 4 2 restall_s
```

3.60 restoreVariables

```
This function is as same as popVariables, but it pops the variable from
db.VariableStack
cf. db.where, popVariables, localVariables, debugMode
```

3.61 restriction

```
 [[f1 f2 ...] [t1 t2 ...] [vars params] [k0 k1 limitdeg ]] restriction
  [ 0-th cohomology group,  (-1)-th cohomology group, .... ]

 [[f1 f2 ...] [t1 t2 ...] [vars params] limitdeg] restriction

This function can be used by loading the experimental package cohom.sm1.
Restriction of the D-ideal [f1 f2 ...] to t1=0, t2=0, ... is computed.
vars is a list of the variables and params is a list of parameters.
k0 is the minimum integral root of the b-function and k1 is the maximum
integral root of the b-function. If these values are not given and
they are small, then they are automatically computed. The program returns
 0-th, ..., -limitdeg-th cohomology groups.
[vars params] and [k0 k1 deg] are optional arguments.
If vars and params are not given, the values of the global variables
```

```
BFvarlist and BFparlist will be used.

For the algorithm, see math.AG/9805006, http://xxx.langl.gov

Example 1: cf. math.AG/9801114, Example 1.4
  [[(- 2 x Dx - 3 y Dy +1) (3 y Dx^2 - 2 x Dy)]
     [(x) (y)] [[(x) (y)] [ ]]] restriction  ::
[    [    0 , [   ]  ]  , [    1 , [   ]  ]  , [    1 , [   ]  ]  ]
       H^0 = 0,     H^(-1)= C^1/(no relation), H^(-2)=C^1/(no relation).
Example 2:
[[(x Dx-1) (Dy^2)] [(y)] [[(x) (y)] [ ]]] restriction ::
[    [    2 , [    -x*Dx+1 , -x*e*Dx+e ]  ]  , [    0 , [   ]  ]  ]
     H^0=D_1^2/([-x Dx+1,0],[0, -x Dx + 1]),  H^(-1) = 0
     where  e^0, e^1, e^2, ..., e^(m-1) are standard basis vectors of
            rank m free module (D_1)^m. D_1 is the ring of differential
            opertors of one variable x.
Example 3:
[[(x Dx-1) (Dy^2)] [(y)] [[(x) (y)] [ ]] 0] restriction ::
Example 4:
[[[(0) (x^2 Dx+x)] [(Dx^2+x Dx^3) (0)]] [(x)] [[(x)] [ ]]] restriction ::
In case of vector input,  RESTRICTION VARIABLES MUST APPEAR FIRST
in the list of variable. We are using wbfRoots to get the roots of
b-functions, so we can use only generic weight vector for now.
```

3.62 rrank

```
 a rrank b
 array a;  number b
It computes the holonomic rank for regular holonomic system.
For the algorithm, see Grobner deformations of hypergeometric differential equations, 1999, Springer.
Chapter 2.
Example 1 :
 [ [( (x Dx)^2 + ( y Dy)^2) ( x Dx y Dy -1)] (x,y)] rrank ::
```

3.63 saturation

```
[ideal J vlist] saturations jjj
It returns (ideal : J^\infty)
Saturation is computed in the ring of polynomials.
When J=[f_1, f_2, ...], it is equal to
((ideal, z-(f_1 + y f_2 + y^2 f_3 +...)) : z^\infty) \cap k[x].
Example 1:
           [[(x1 y1 + x2 y2 + x3 y3 + x4 y4)
             (x2 y2 + x4 y4) (x3 y3 + x4 y4) (y1 y4 - y2 y3)]
            [(y1) (y2) (y3) (y4)] (x1,x2,x3,x4,y1,y2,y3,y4)] saturation
            /ff set [ff (x1,x2,x3,x4,y1,y2,y3,y4)
                     [[(y1) 1 (y2) 1 (y3) 1 (y4) 1]]] pgb
            0 get [(y1) (y2) (y3) (y4)] eliminatev ::
Example 2: [[(x2^2) (x2 x4) (x2) (x4^2)] [(x2) (x4)] (x2,x4)] saturation
```

3.64 syz

```
a syz [b c]
```

```
array a; array b; array c
b is a set of generators of the syzygies of f.
c = [gb, backward transformation, syzygy without dehomogenization].
See groebner.
a : [f ];    array f;  f is a set of generators of an ideal in a ring.
a : [f v];   array f; string v;  v is the variables.
a : [f v w]; array f; string v; array of array w; w is the weight matirx.
 v may be a ring object.
Example 1: [(x,y) ring_of_polynomials 0] define_ring
           [ [(x^2+y^2-4). (x y -1).] ] syz ::
Example 2: [ [(x^2+y^2) (x y)]   (x,y)  [ [(x) -1 (y) -1] ] ] syz ::
Example 3: [ [( (x Dx)^2 + (y Dy)^2 -1) ( x y Dx Dy -1)] (x,y)
             [ [ (Dx) 1 ] ] ] syz pmat ;
Example 4:  [ [(2 x Dx + 3 y Dy+6) (2 y Dx + 3 x^2 Dy)] (x,y)
             [[(x) -1 (Dx) 1 (y) -1 (Dy) 1]]] syz pmat ;
Example 5:  [ [ [(x^2) (y+x)] [(x+y) (y^3)] [(2 x^2+x y) (y+x+x y^3)]]
              (x,y) ] syz pmat ;
Example 6:  [ [ [(x^2) (y+x)] [(x+y) (y^3)] [(2 x^2+x y) (y+x+x y^3)]]
              (x,y) [[(x) -1 (y) -2]] ] syz pmat ;
Example 7:  [ [ [(0) (0)] [(0) (0)] [(x) (y)]]
              [(x) (y)]] syz pmat ;
```

3.65 tensor0

```
 [F G vlist] tensor0
This function requires the package cohom.sm1.
Example 1:
 [[(2 x Dx - 1)] [(2 x Dx - 3)] (x)] tensor0
Example 2:
 [[(-x*Dx^2+x-Dx+1)] [((x Dx + x +1)(Dx-1))] (x)] tensor0
Example 3:
 [[(x Dx -1) (y Dy -4)] [(Dx + Dy) (Dx-Dy^2)] (x,y)] tensor0
```

3.66 usePolymake.OoHG.curl

```
doPolymake = doPolymake.OoHG with cgiQueryPolymake.curl
It should be used when cgiQueryPolymake.native does not work
over, e.g., a reverse proxy.
The command curl is required.  cf. cgi.verbose, doPolymake.OoHG
hostname is set in cgiQueryPolymake.hostname
cginame is set in  cgiQueryPolymake.cginame
```

3.67 usePolymake.OoHG.native

```
doPolymake = doPolymake.OoHG with cgiQueryPolymake.native
cf. doPolymake.OoHG
hostname is set in cgiQueryPolymake.hostname
cginame is set in  cgiQueryPolymake.cginame
```

3.68 usePolymake.local

```
doPolymake calls local polymake
```

3.69 wIntegration0

```
 [gg vlist weight] wIntegration0  [ igg bb]
list of strings gg; list of strings vlist;
list weight;
integer k1;
list of polys igg; list of polys base;
gg are input ideal or submodule.
igg are relations and bb are bases. They give the integral.
This function fails when weight is not generic.
cf. intwbf, intwbfRoots, integral-k1.
This function is defined in intw.sm1 and requires oxasir.sm1 and ox_asir server.
See Grobner Deformations of Hypergeometric Differential Equations, Springer
    Section 5.5 for the algorithm.
Example 1: [ [(Dt - (3 t^2-x)) (Dx + t)] [(t) (x)] [(t) -1 (Dt) 1]]
              wIntegration0
Example 2: [[(-3 x^2 Dy-2 y Dx) (2 x Dx+3 y Dy+6)] [(x) (y)]
            [(x) -1 (Dx) 1 (y) -2 (Dy) 2]]  wIntegration0
           The output [[-x, 1] [x,1]] implies the integral is
           (K x + K 1)/(K (-x) + K 1) = 0 where K is the base field and
           x and 1 is the vector space basis.
           Note that the order of weight and the order of the variables
           must be the same.  Note also that the next of (x) must be (Dx)
           and so on.
```

3.70 wRestriction0

```
 [gg vlist weight] wRestriction0  [ igg bb]
list of strings gg; list of strings vlist;
list weight;
integer k1;
list of polys igg; list of polys base;
gg are input ideal or submodule.
igg are relations and bb are bases. They give the 0-th restriction.
This function fails when weight is not generic.
cf. intwbf, intwbfRoots, integral-k1.
This function is defined in intw.sm1 and requires oxasir.sm1 and ox_asir server.
See Grobner Deformations of Hypergeometric Differential Equations, Springer
    Section 5.5 for the algorithm.
Example 1: [ [(Dt^2) (Dx^2)] [(t) (x)] [(t) -1 (Dt) 1]]
              wRestriction0
Example 2: [[(Dx^2) (Dy^2)] [(x) (y)]
            [(x) -1 (Dx) 1 (y) -2 (Dy) 2]]  wRestriction0
           The output [[-Dx, 1] [Dx,1]] implies the restriction is
           (K Dx + K 1)/(K (-Dx) + K 1) = 0 where K is the base field and
           Dx and 1 is the vector space basis.
           Note that the order of weight and the order of the variables
           must be the same.  Note also that the next of (x) must be (Dx)
           and so on.
```

3.71 wTensor0

```
[F G v weight] wTensor0
See tensor0
It calls wRestriction0 instead of restriction.
Example 1:
 [[(x Dx -1) (y Dy -4)] [(Dx + Dy) (Dx-Dy^2)] (x,y) [1 2]] wTensor0
```

3.72 wbf

```
[[f1 ... fm] [v1 ... vn] [v1 w1 ... vp wp]] wbf [g1 ... gq]
<poly>|<string> f1 ...fm; <string> v1 ... vn;
<string> v1 ... vp; <integer> w1 ... wp;
<poly> g1 ... gq;
f1 ... fm are generators, v1 ... vn are variables,
w1 is the weight of the variable v1, ...
THE ORDERS OF INTEGRAL VARIABLES MUST BE SAME BOTH IN THE SECOND AND
THE THIRD ARGUMENTS. INTEGRAL VARIABLES MUST APPEAR FIRST.
If the weight is not generic, then the function exits with error.
cf. bf-111 for w=(1 1 1 1 ...)
Example 1: [[(x-y) (Dx+Dy)] [(y) (x)] [(y) -1 (Dy) 1]] wbf
            restrict only for y.
Example 2: [[(-3 x^2 Dy-2 y Dx) (2 x Dx+3 y Dy+6)] [(x) (y)]
            [(x) -1 (Dx) 1 (y) -2 (Dy) 2]] wbf
Example 3: [[[(0) (x^2 Dx+x)] [(Dx^2+x Dx^3) (0)]] [(x)]
            [(x) -1 (Dx) 1]] wbf
```

3.73 wbfRoots

```
This function needs oxasir  --- rationalRoots2
This function is defined in intw.sm1 and requires oxasir.sm1 and ox_asir server.
Example 1:  [[(-3 x^2 Dy-2 y Dx) (2 x Dx+3 y Dy+6)] [(x) (y)]
             [(x) -1 (Dx) 1 (y) -2 (Dy) 2]] wbfRoots
Example 2:   [[[(0) (x^2 Dx+x)] [(Dx^2+x Dx^3) (0)]] [(x)]
               [(x) -1 (Dx) 1]] wbfRoots
```

3.74 wdeRham0

```
It computes the midle dimensional cohomology groups and bases.
A generic weight vector is used for the computation.
This function is defined in intw.sm1 and requires oxasir.sm1 and ox_asir server.
 Example 1 : [(x^3-y^2) (x,y) [(x) -1 (Dx) 1 (y) -2 (Dy) 2]] wdeRham0
 Example 2 : [(x^3+y^3+z^3) (x,y,z)
      [(x) -1 (Dx) 1 (y) -2 (Dy) 2 (z) -3 (Dz) 3]] wdeRham0
 Example 3 : [(x^3 -y z^2) (x,y,z)
      [(x) -1 (Dx) 1 (y) -2 (Dy) 2 (z) -3 (Dz) 3]] wdeRham0
 Example 4 : [(x^3 -y^2 z^2) (x,y,z)
      [(x) -1 (Dx) 1 (y) -2 (Dy) 2 (z) -3 (Dz) 3]] wdeRham0
```