

Pfpcoh (cohomology/homology groups for $p \leq q$) Manual

Edition : auto generated by oxgentexi on 1 May 2025

1 Cohomology group associated to pF_q

This section describes functions to evaluate invariants associated to (co)homology groups of the hypergeometric functions pF_q (${}_pF_q$)

In order to use the functions in this section in OpenXM/Risa/Asir, executing the commands

```
load("pfpcoh.rr")$ load("pfphom.rr")$
is necessary at first.
```

1.0.1 pfp_omega

`pfp_omega(P)`

: It returns the Gauss-Manin connection Omega for the generalized hypergeometric function $P F_{P-1}(aa_1, aa_2, \dots; cc_1, cc_2, \dots; x)$.

Description:

Define a vector valued function Y of which elements are generalized hypergeometric function $f_1=F$ and $f_2=xd f_1/dx$, $f_3=xd f_2/dx$, ... It satisfies $dY/dx = \Omega Y$. Generalized hypergeometric function is defined by the series $p F_{p-1}(aa_1, aa_2, \dots; cc_1, cc_2, \dots; x) = \sum_{k=0, \infty} (aa_1)_k (aa_2)_k \dots / (1)_k (cc_1)_k (cc_2)_k \dots x^k$

Example:

```
pfp_omega(3);
```

1.0.2 pfpcoh_intersection

`pfpcoh_intersection(P)`

: `pfpcoh_intersection(P)` returns an intersection matrix for cocycles associated to the generalized hypergeometric function $p F_{p-1}$.

Description:

This program `pfpcoh.rr` computes an intersection matrix S of cocycles of $p F_{p-1}$ and compares it with the matrix obtained by solving a differential equation for intersection matrix.

Algorithm:

Ohara, Sugiki, Takayama, Quadratic Relations for Generalized Hypergeometric Functions $p F_{p-1}$

Example:

```
load("pfpcoh.rr")$
S=pfpcoh_intersection(3);
```

Author : K.Ohara

1.0.3 pfphom_intersection

`pfphom_intersection(P)`
: intersection matrix of homology cycles.

Description:

Computing intersection matrix of cycles associated to $p F_{-(p-1)}$. As to the meaning of parameters $c_1, c_2, c_3, \dots$, see the paper Ohara, Kyushu J. Math. Vol. 51 PP.123.

Algorithm:

Ohara, Sugiki, Takayama, Quadratic Relations for Generalized Hypergeometric Functions $p F_{p-1}$

Example:

```
SS = pfphom_intersection(3)$
```

You get the intersection matrix of homologies for $3 F_2$.

Author : K.Ohara

1.0.4 pfphom_monodromy_pair_kyushu

`pfphom_monodromy_pair_kyushu(P)`
:

Description:

It returns the pair of monodromy matrices.

Algorithm:

Ohara, Kyushu J. Math. Vol.51 PP.123 (1997)

Example:

```
MP = pfphom_monodromy_pair_kyushu(3)$
```

You get a pair of monodromy matrices for $3F_2$ standing for two paths encircling 0 and 1.

Index

(Index is nonexistent)

(Index is nonexistent)

Short Contents

1 Cohomology group associated to pF_q	1
Index	3

Table of Contents

1	Cohomology group associated to pFq.....	1
1.0.1	pf ω	1
1.0.2	pfcoh_intersection.....	1
1.0.3	pfphom_intersection.....	2
1.0.4	pfphom_monodromy_pair_kyushu.....	2
Index.....		3

